

# Numerical simulations of cosmic structures

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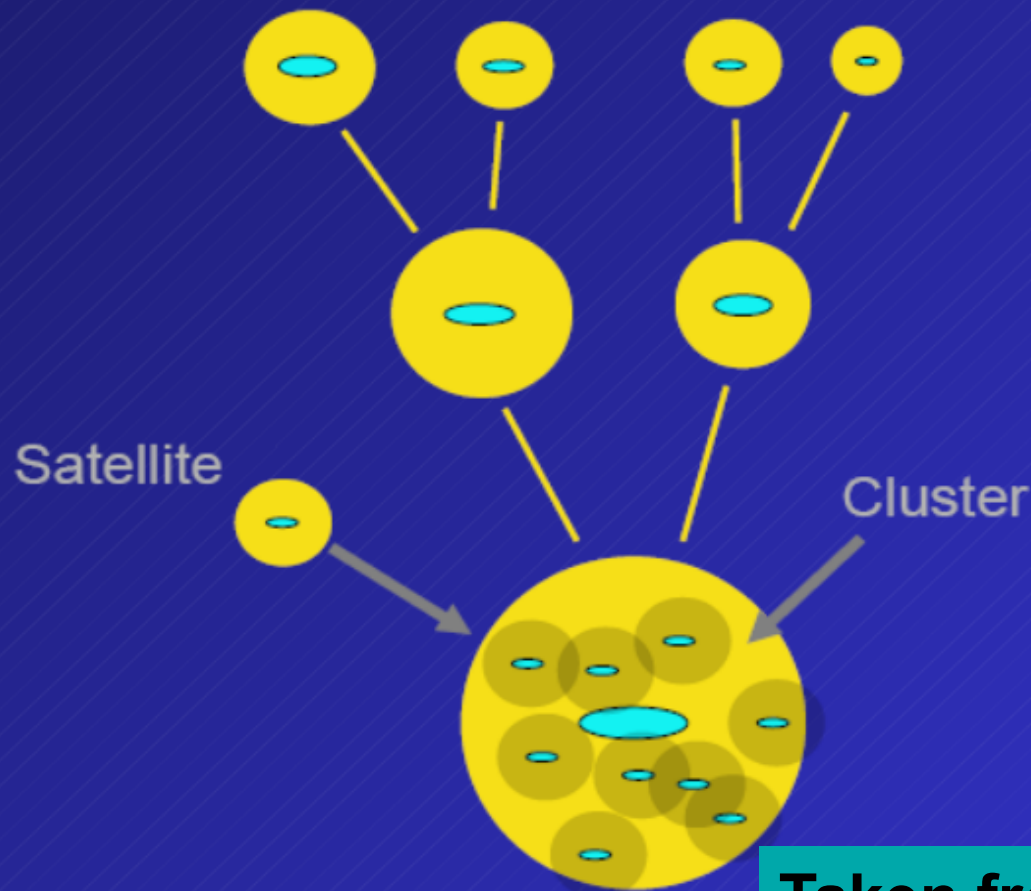
Many Collaborators in SJTU and  
SHAO

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岚)

# Theoretical framework for understanding evolution of galaxies and dark matter halos

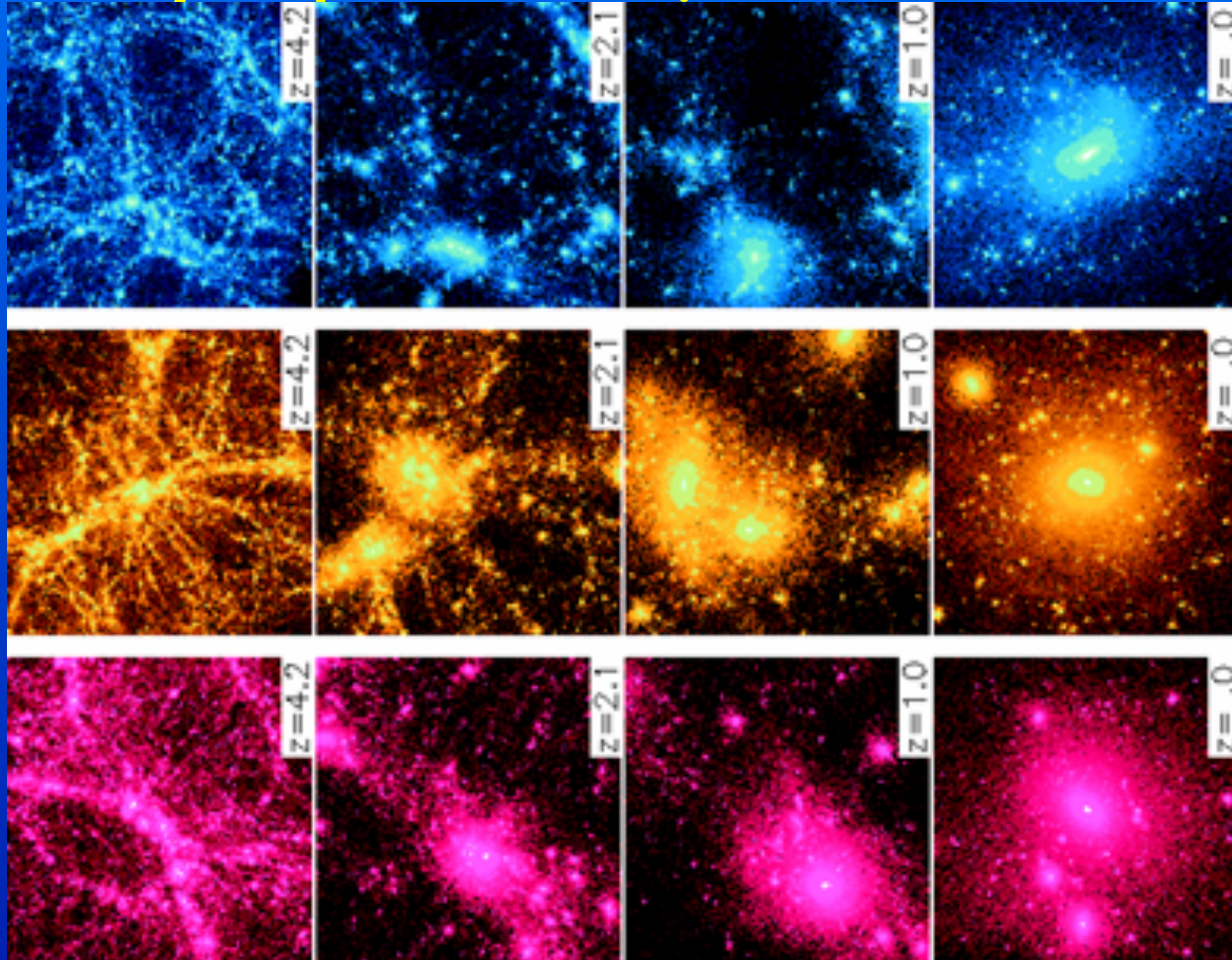
## A third key component: satellites vs. centrals

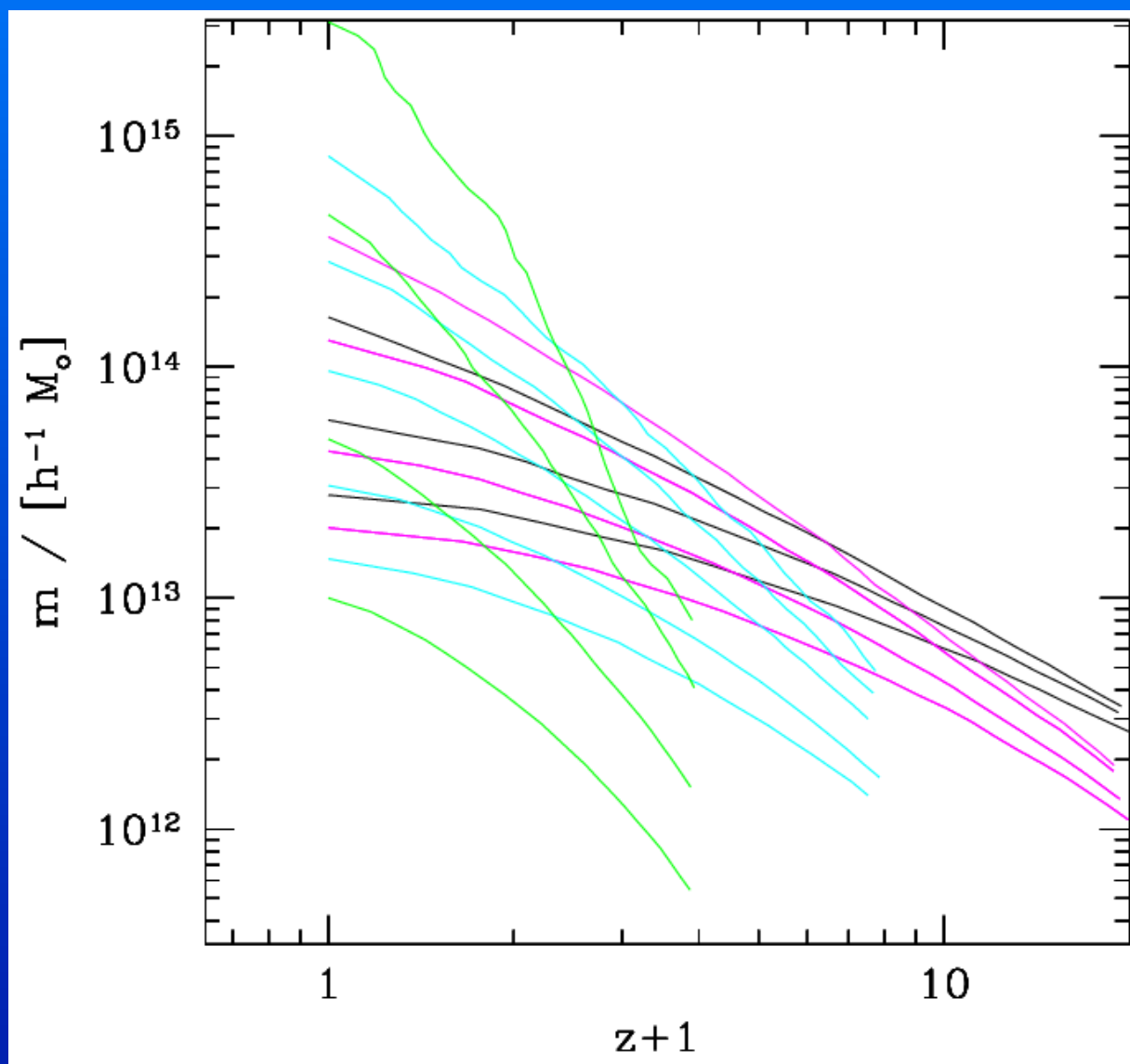
Smaller satellite galaxies can orbit for a time within larger halos without merging onto the central galaxies.



Taken from S. Faber

# The universal mass accretion history of dark matter haloes

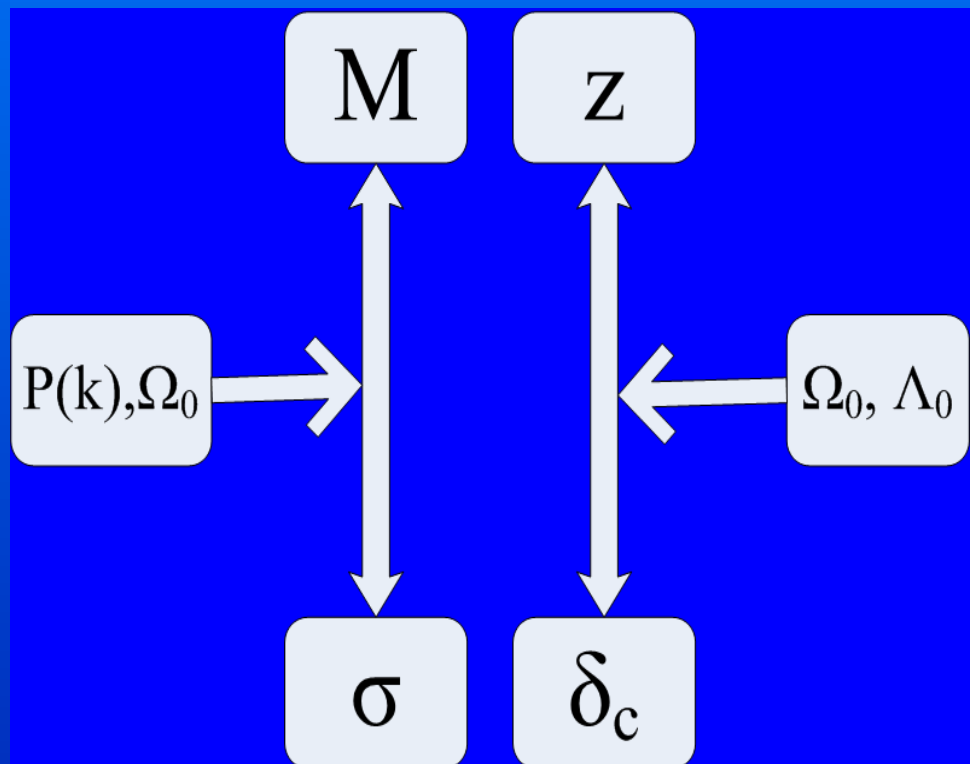




# Choosing proper variables for modeling

- Given cosmology and power spectrum, after extrapolated linearly to  $z=0$ , linear mass variance of given volume  $\sigma$  is determined by  $M$ , and  $\sigma(M) \equiv \sigma'(M, z) / D(z)$  linear critical collapse overdensity  $\delta_c$  by  $z$ .

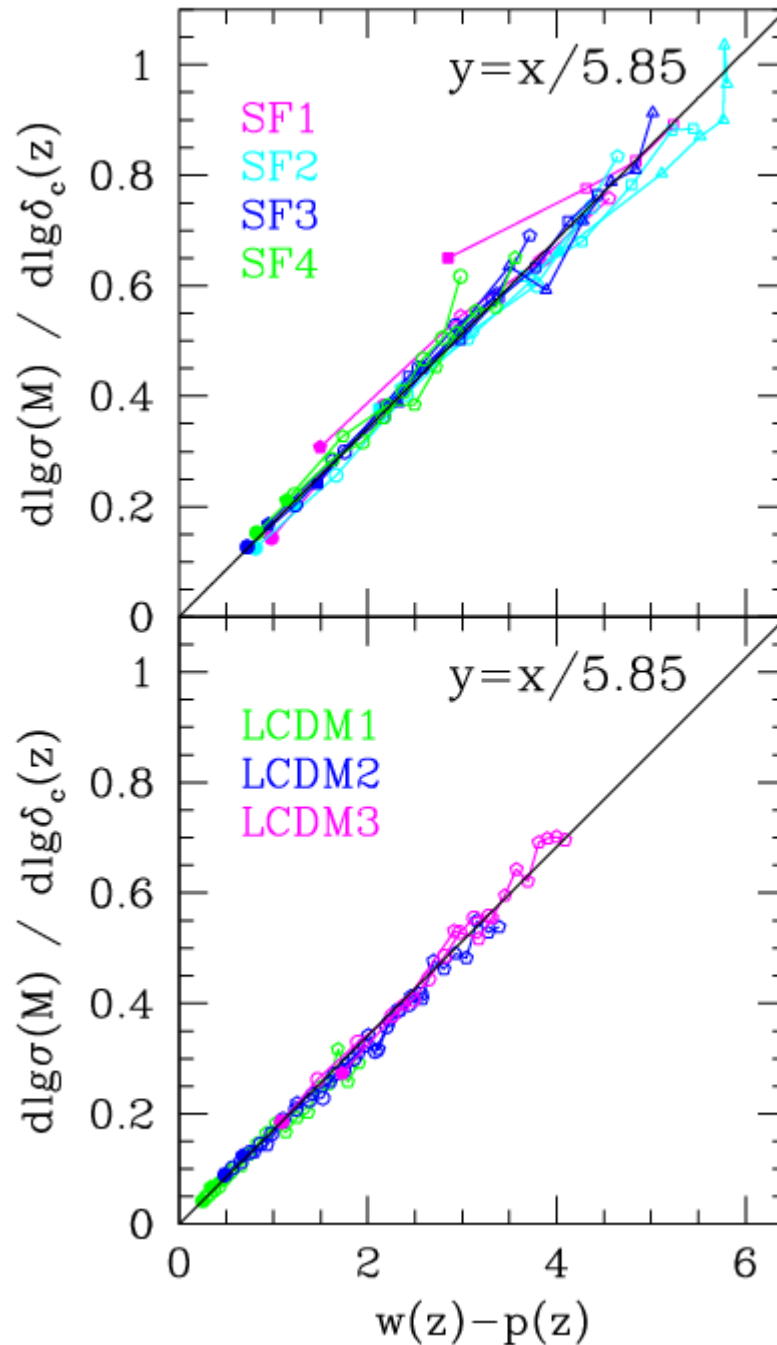
$$\delta_c(z) \equiv \delta'_c(\Omega_m(z), \Omega_\Lambda(z)) / D(z)$$



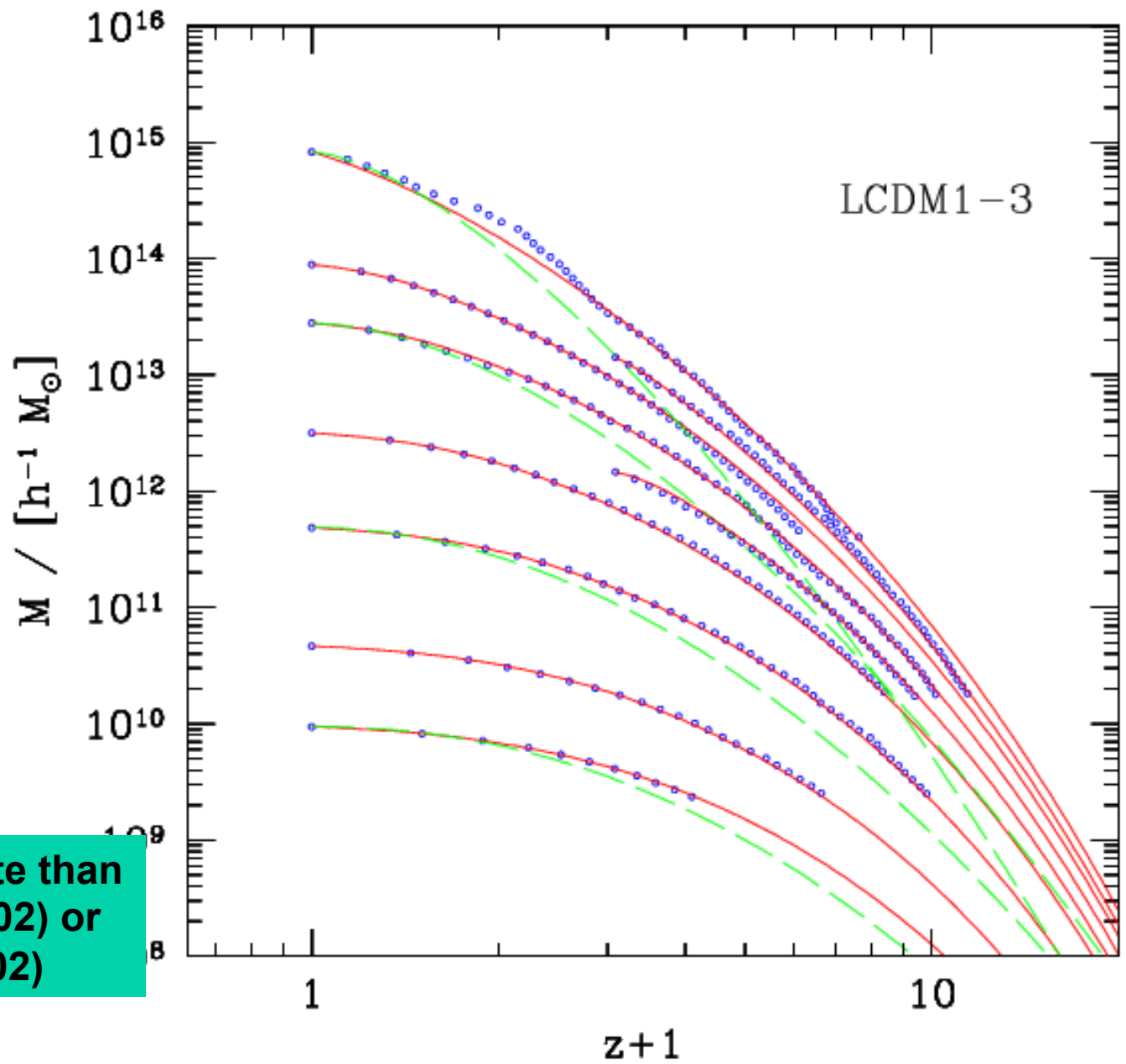
# Universal differential relation

$w$ - $p$  determines growth rate of halo of mass  $M$

D.H. Zhao, et al. ApJ (2009)



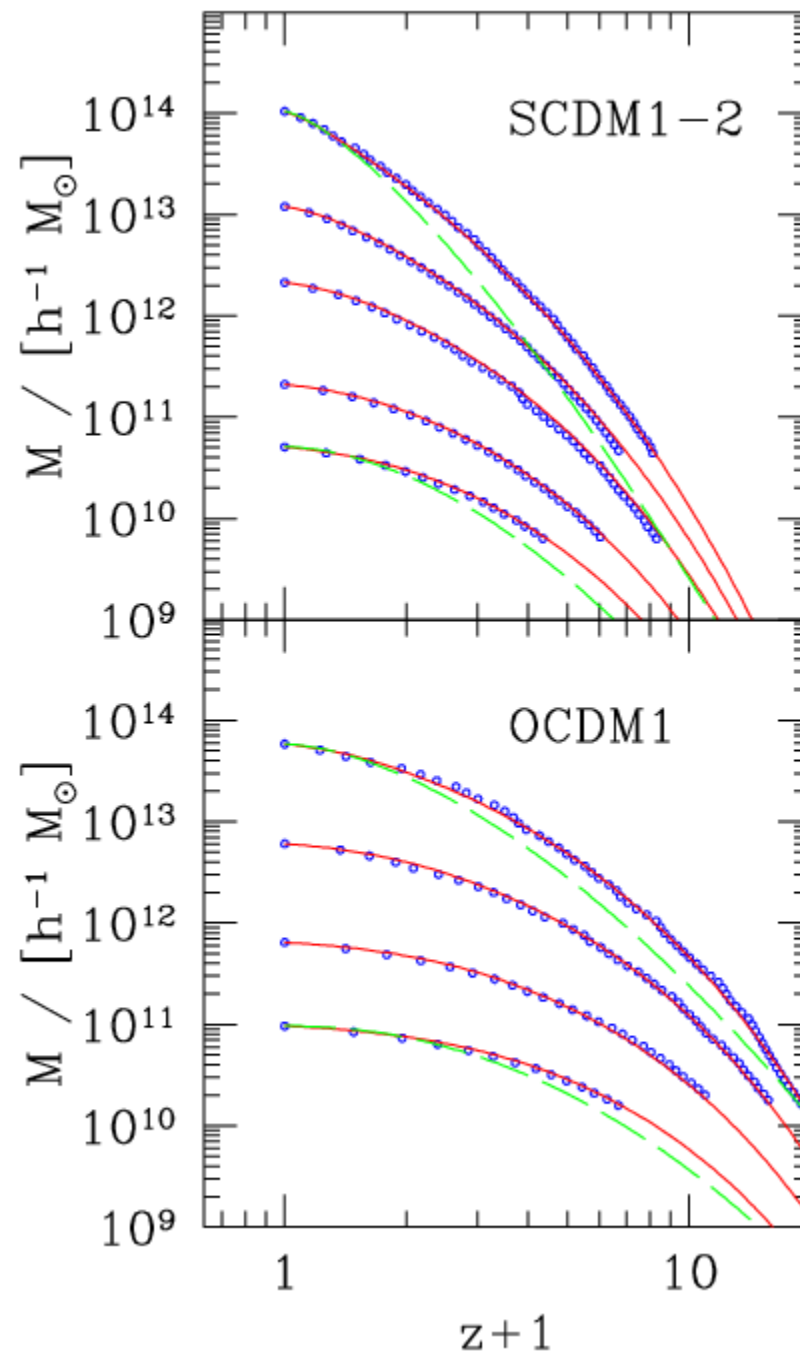
- LCDM



Much more accurate than  
van den Bocsh (2002) or  
Wecshler et al. (2002)



- SCDM  
&  
OCDM

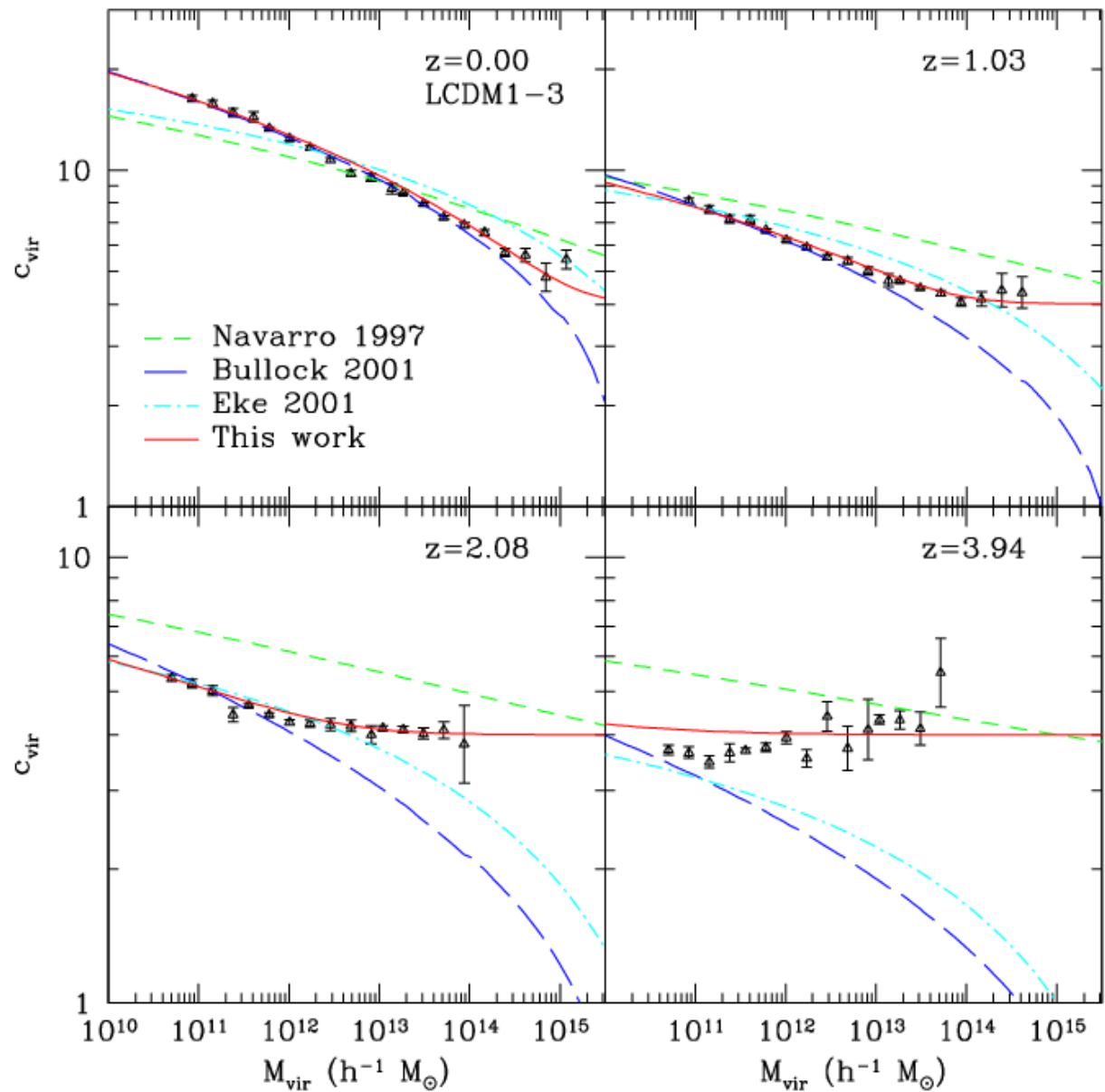




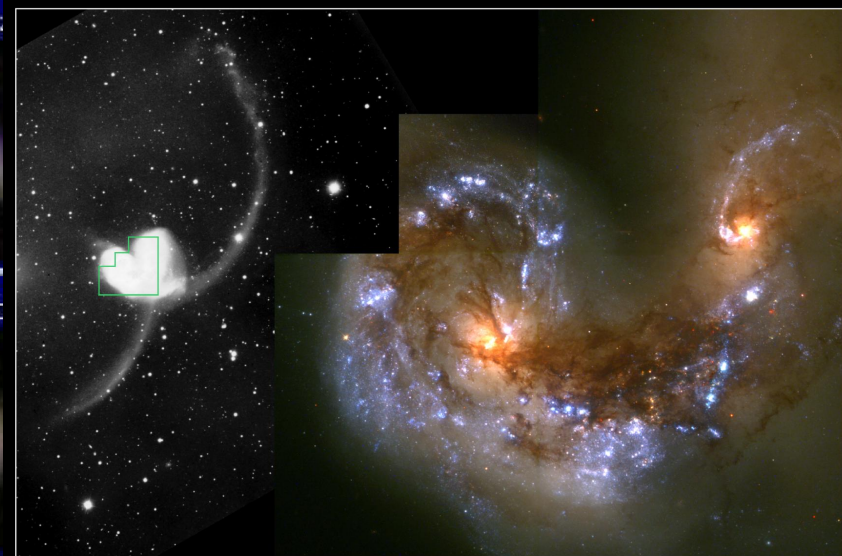
# Evolution of halo density profile

- Combined with MAHs model we presented in part I, c- $t$  correlation can be used to predict the evolution of halo density profile

- LCDM1-3



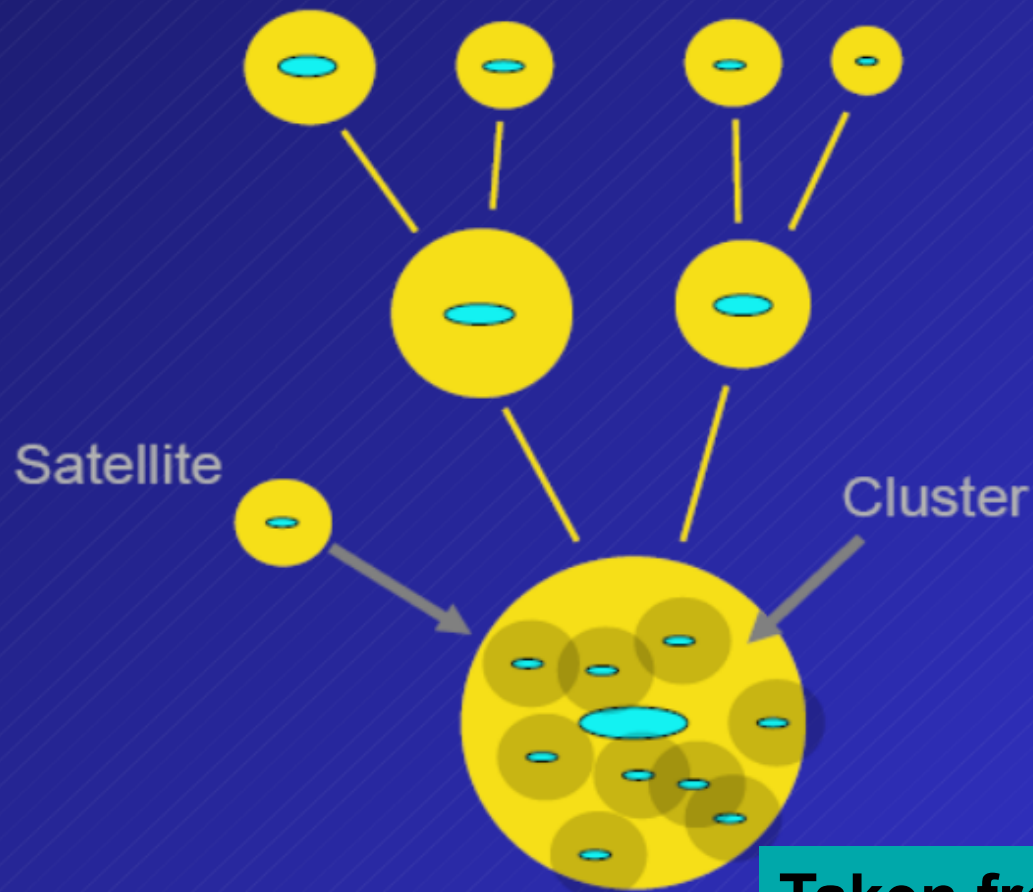
# Merging of galaxies



# Theoretical framework for understanding evolution of galaxies and dark matter halos

## A third key component: satellites vs. centrals

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Taken from S. Faber

- We employed a parallel version of the SPH code GADGET 2(Springel 2005). The box is  $100h^{-1}M_{pc}$  on a side, with  $512^3$  dark matter particles and  $512^3$  gas particles. Gravity is softened with a spline, roughly equivalent to a Plummer force softening of  $4.9h^{-1}$  comoving kpc. There are totally 177 snapshots from  $z=19$ , among which 28 are before  $z=3.5$ , and 149 are at  $z \leq 3.5$ .

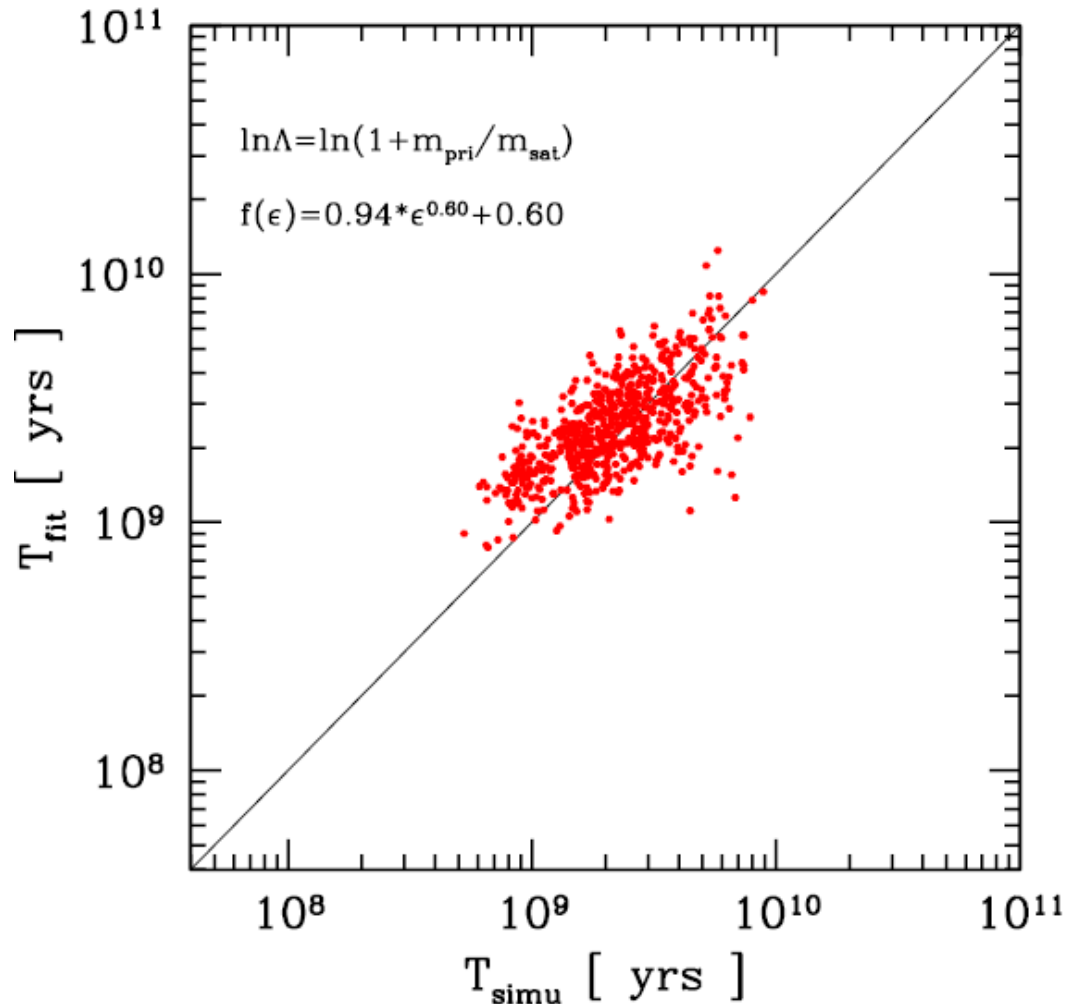
present time  $z = 0$  with an equal logarithmic scale factor interval  $\Delta \ln a = 0.01$  between two consecutive outputs. The large number of the outputs enables us to accurately sample orbits of satellites within massive haloes, with about 8 outputs for one dynamical crossing time. Both the good force resolution and the dense sampling of snapshots are crucial for the current study.

# Two types of merger timescales in literature

- The time duration for a satellite falling into the central galaxy from the first crossing of the virial radius of host DM halo; important of theoretical modeling, such as in SAMs;
- The time duration for a close pair of galaxies at a fixed separation (small) to merge; important for observations



$$T_{\text{fit}} = \frac{0.90\epsilon^{0.47} + 0.60}{2C} \frac{m_{\text{pri}}}{m_{\text{sat}}} \frac{1}{\ln[1 + (\frac{m_{\text{pri}}}{m_{\text{sat}}})]} \frac{\sqrt{r_{\text{vir}} r_c}}{V_c}, \quad (8)$$



Corrections:

- 1) **Mass loss**: a factor of 2 longer
- 2) **Motion of the central galaxies and dynamical evolution**: weak dependence on  $\epsilon$  (orbital circularity)
- 3) **Dependence on the DM mass of the primary and satellite**: the Coulomb logarithm
- 4) **Scatter**: 40% reflecting hierarchical formation and diversity of host halos

**Merger timescale for all mergers**

# The second merger timescale

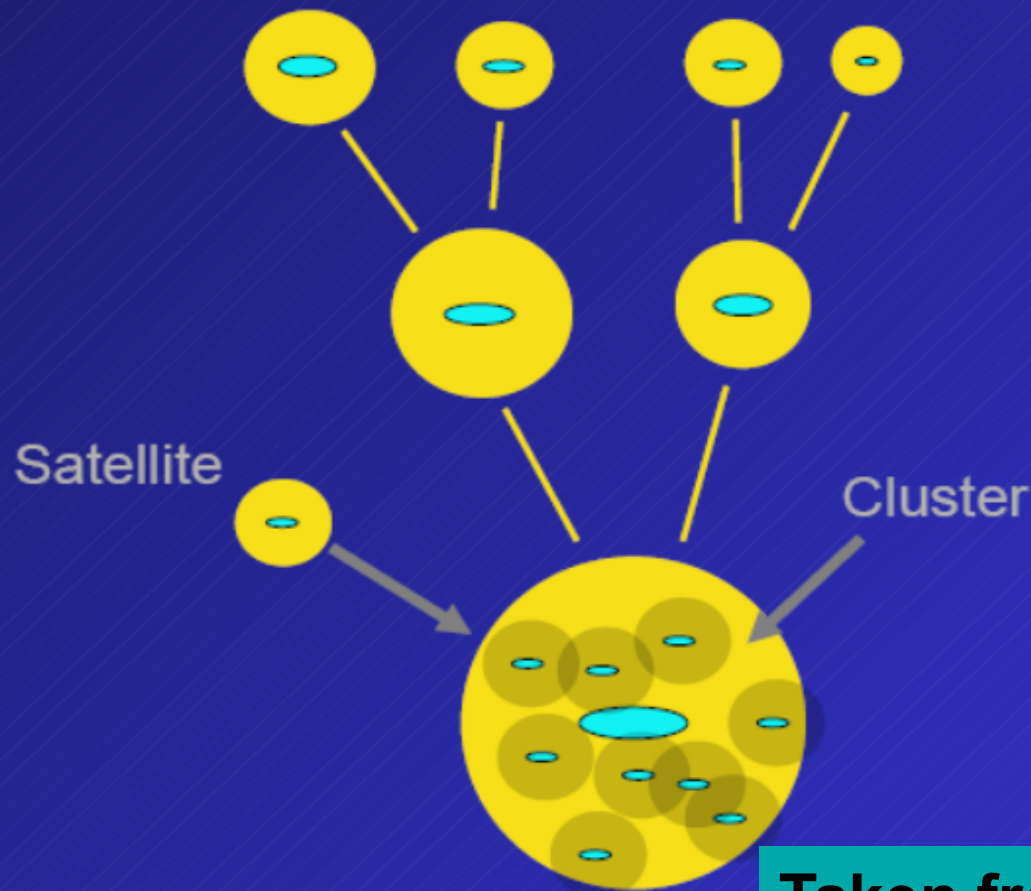
- A merger time for close pairs of certain mass (luminosity) and separation, related to measure the merger rate from the counts of close pairs in observations
- (Jiang, YPJ, Han, 2013, [astroph/1307.3322](#))



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# Some scaling considerations

$$T_{\text{fit}} = \frac{0.90\epsilon^{0.47} + 0.60}{2C} \frac{m_{\text{pri}}}{m_{\text{sat}}} \frac{1}{\ln[1 + (\frac{m_{\text{pri}}}{m_{\text{sat}}})]} \frac{\sqrt{r_{\text{vir}} r_c}}{V_c}, \quad (8)$$

Considering  $v_c \approx \sqrt{\frac{Gm_{1,v}}{r_{1,v}}}$  in the primary halo,

$$T_{\text{mg}} \propto \frac{m_{1,v}^{1/2} r_p^2}{G^{1/2} m_2 \ln \Lambda r_{1,v}^{1/2}}.$$

The volume merger rate can be written as

$$\Phi = C_{\text{mg}} n_1 n_p(< r_p) / T_{\text{mg}},$$

Replacing  $T_{\text{mg}}$  in equation (1) with equation (2),  
obtain

$$\Phi = A_* \frac{G^{1/2} m_2 r_{1,v}^{1/2} n_1 n_p(< r_p)}{m_{1,v}^{1/2} r_p^2}.$$

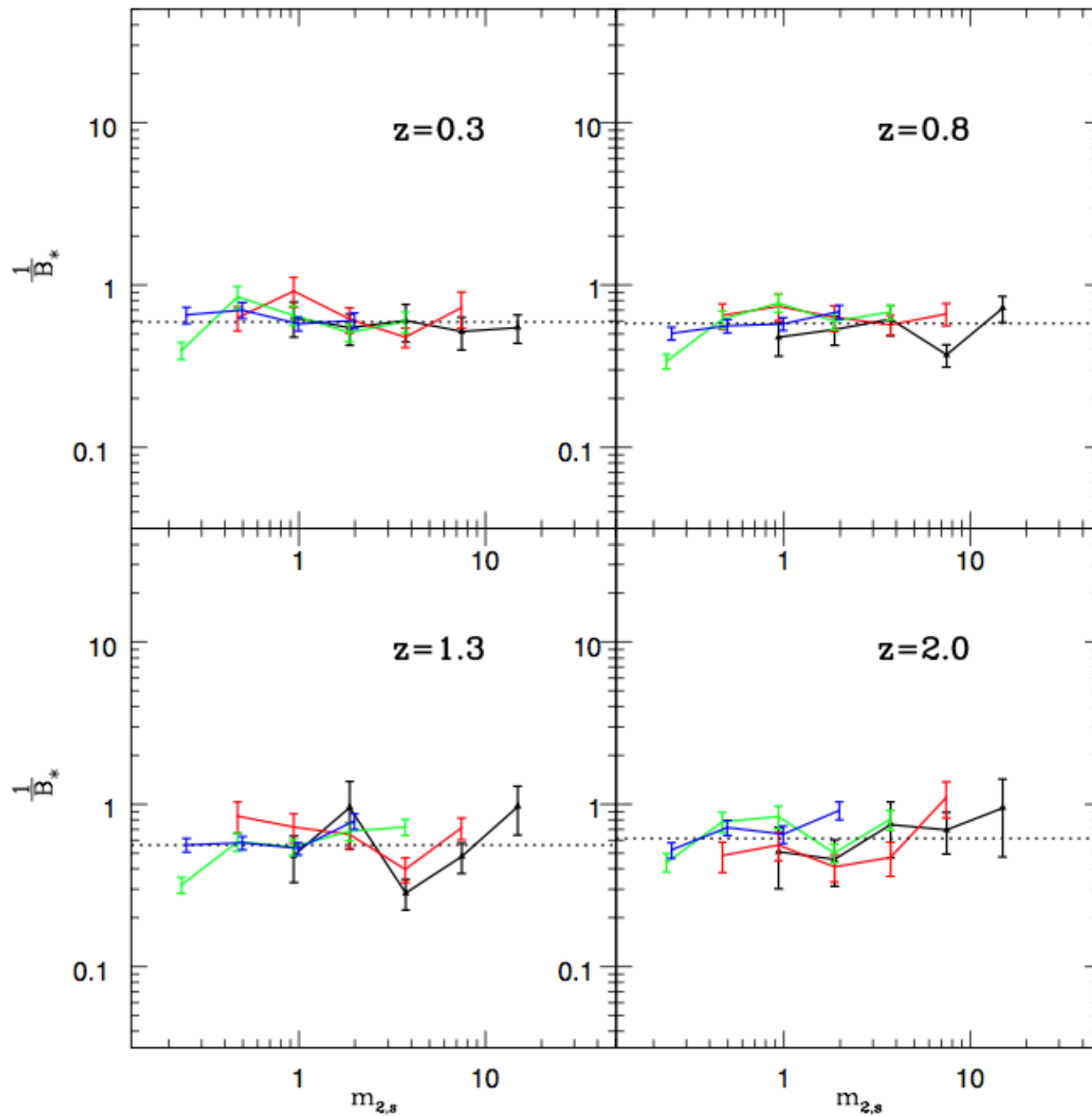
# More scaling considerations

- The retained mass of the satellite:  $m_{2,v} \frac{r_p}{r_{1,v}}$ 
  - Correct when DM halo is an isothermal sphere of; but good for real DM halos
- With the definition of halos (200 critical density) and cosmological parameter relations we have

$$T_{\text{mg}} \propto \frac{m_{1,v}}{m_{2,v}} [m_{1,v} G H_0 E(z)]^{-1/3} r_p$$

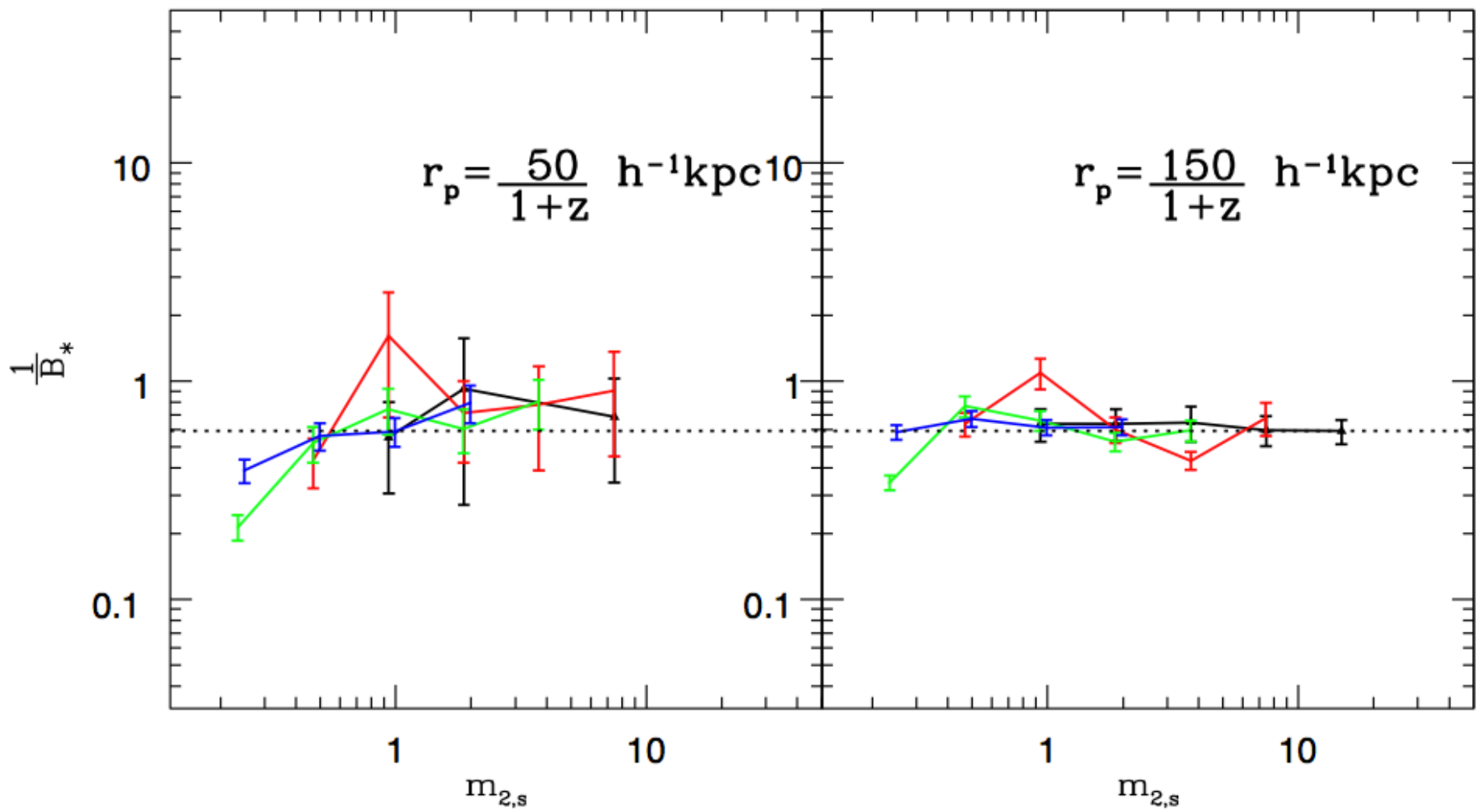
$$\Phi = B_* \frac{m_{2,v} n_1 n_p(< r_p) [m_{1,v} G H_0 E(z)]^{1/3}}{m_{1,v} r_p}.$$

$E(z) = \Omega_\Lambda + \Omega_m(1+z)^3$  : dimensionless Hubble parameter  
(i.e.  $H(z)$  in unit of  $H_0$ )



When the retained mass is considered for the satellites:

- 1) For different masses of central and satellites
- 2) For different redshifts



for the different separations

# Applications to observations

- Measure the pair count per unit volume of stellar masses  $m_{1,s}$  and  $m_{2,s}$  (or luminosities)  $N_p(< r_p) = n_1 n_p(< r_p)$ 
  - $n_1$  is the density of galaxy 1 and  $n_p$  is the number count within projected  $r_p$  (corrected for the background) of galaxies 2 around galaxy 1
- Volume merger rate:  $\Phi = N_p(< r_p)/T_{\text{mg}}$  ;
- Merger rate of G 1 and G 2:  $n_p(< r_p)/T_{\text{mg}}$

$$T_{\text{mg}}(< r_p^{\text{proj}}) = \frac{10^{-0.23}}{0.66} \frac{m_{1,v}}{m_{2,v}} [m_{1,v} G H_0 E(z)]^{-1/3} r_p$$