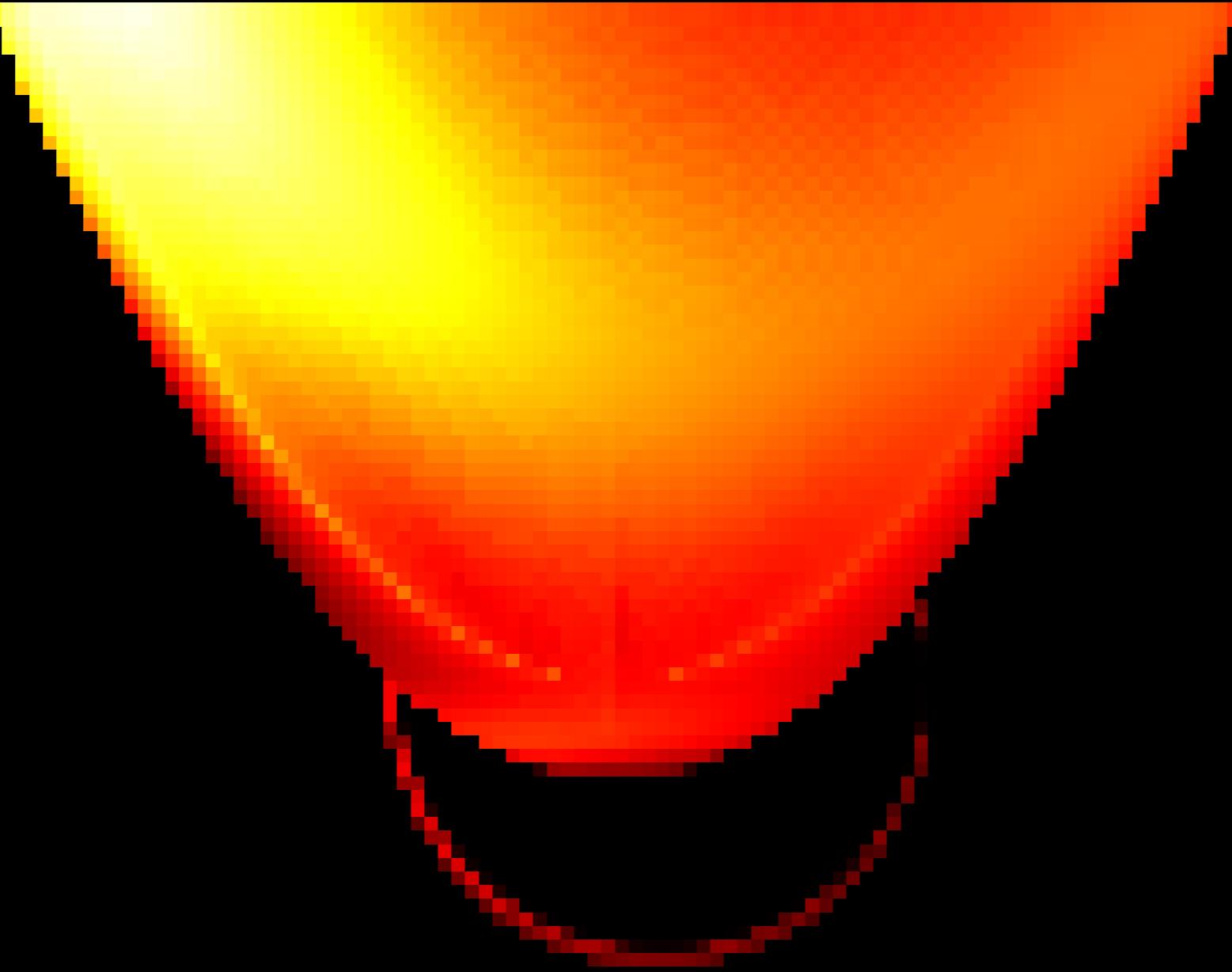


# Semi-analytical GRMHD Jet Model and its Synchrotron Radiation Image on Horizon Scale



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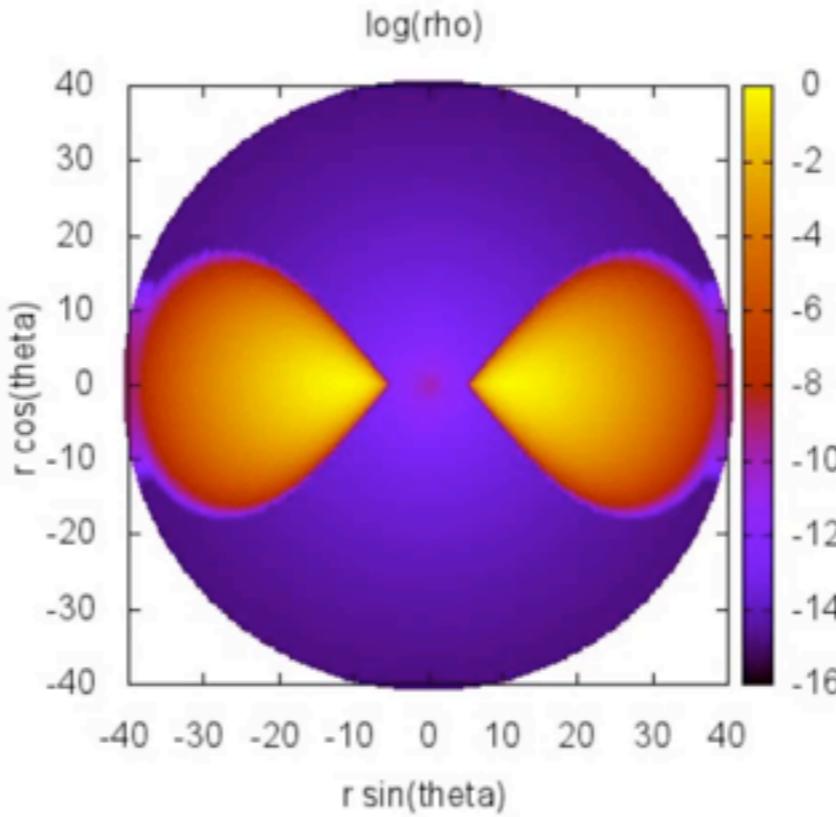
Feb. 8 EAYAM 2015

- 
- why GRMHD ?

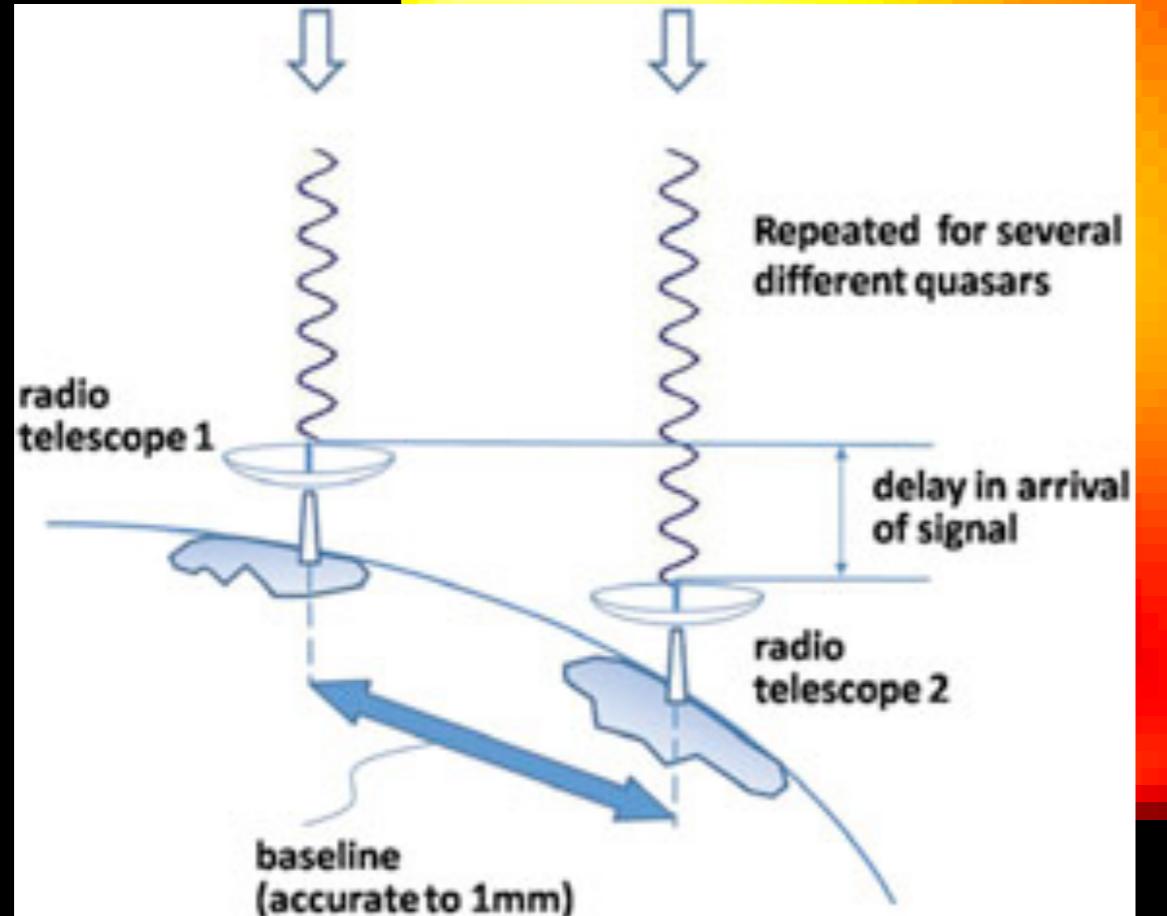
(general relativistic magnetohydrodynamics)

strong gravity + magnetic field + fluid

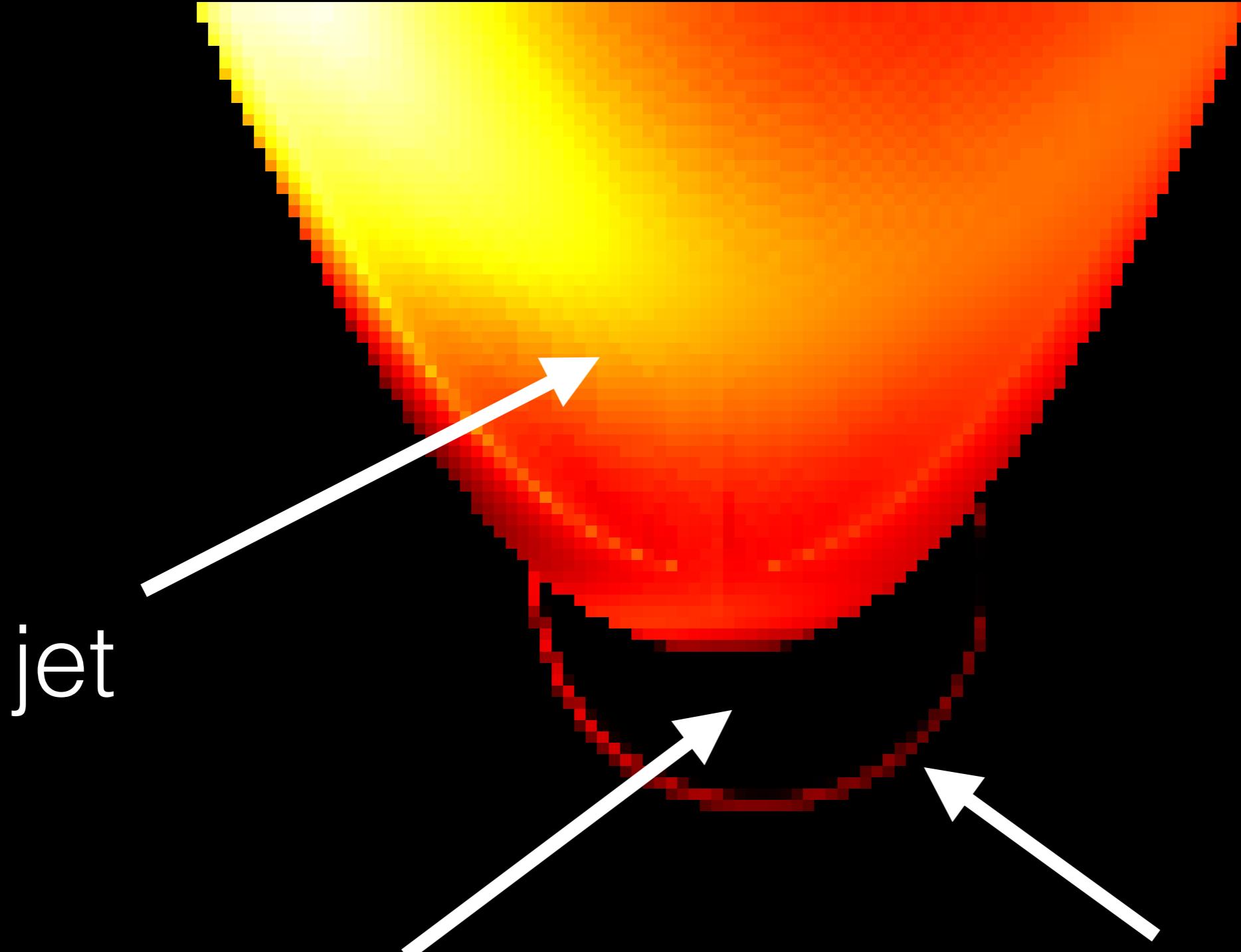
## GRMHD simulation example



- why **semi-analytical** approach?  
to provide a **complementary** understanding of the  
relativistic jets, compared to GRMHD **numerical  
simulations**



- why Radiation Image on horizon scale?  
important for upcoming **sub-mm VLBI observation** (**Very Long Baseline Interferometry**) with microarcsecond resolution



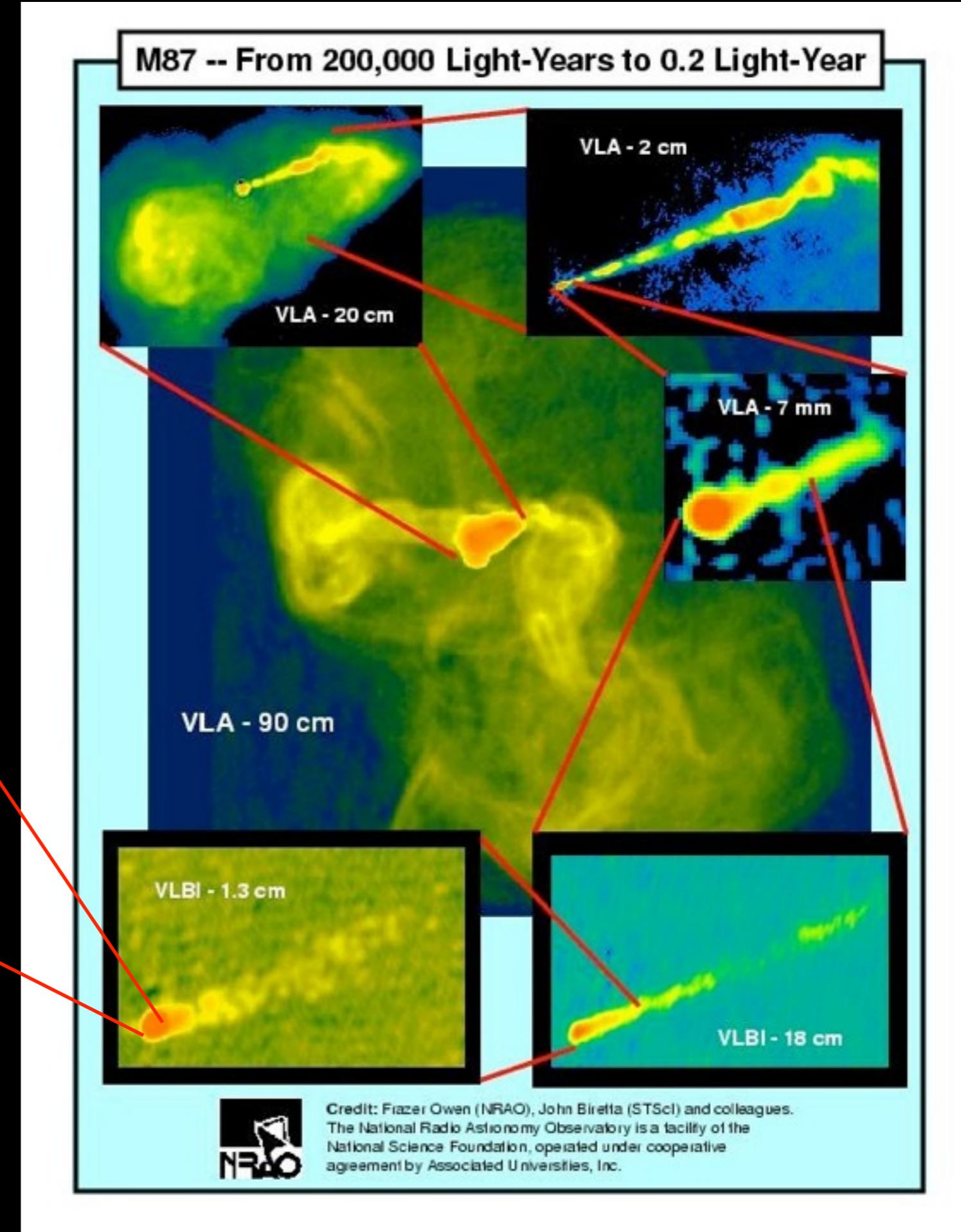
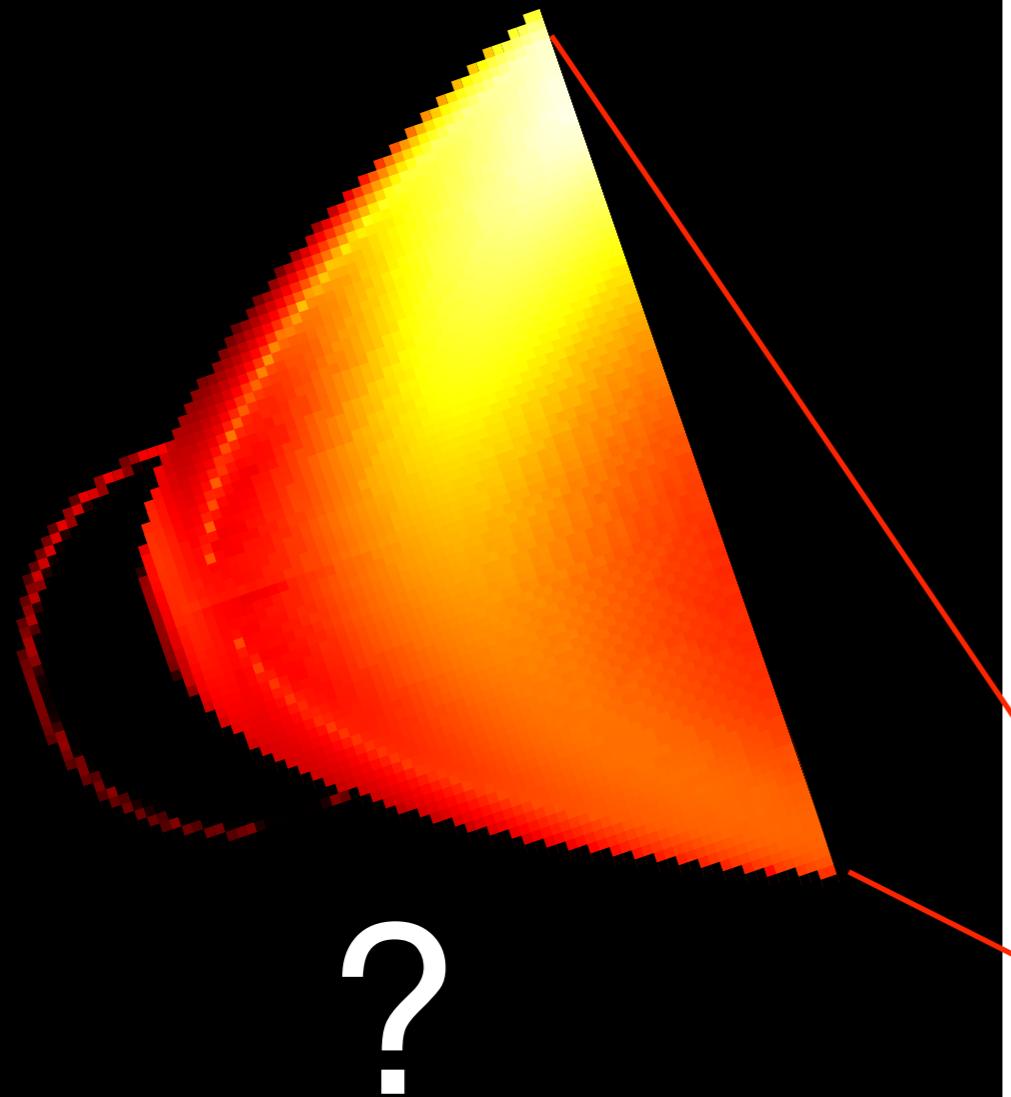
jet

black hole

photon ring due  
to light bending

(theoretical computation; consider only jet component)

future sub-mm VLBI  
observation  
(micro-arcsec scale)!!

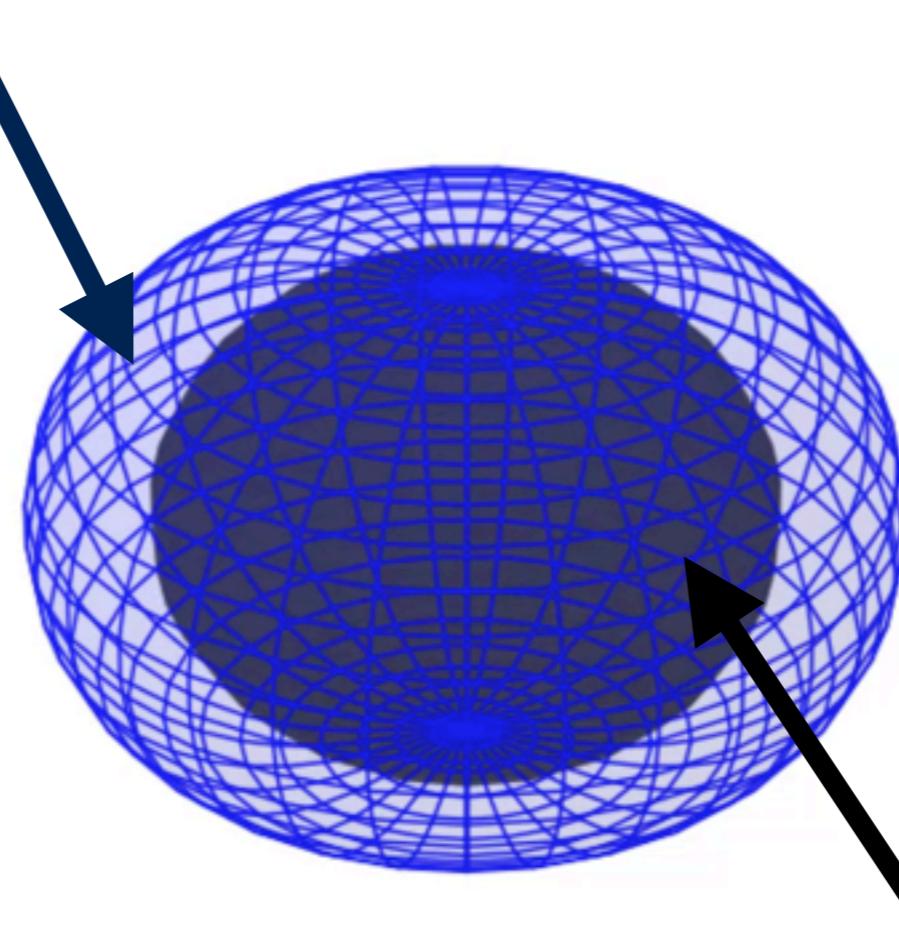


# Outline

- GRMHD jet model
  - jet launching at the expense of black hole rotational energy
  - semi-analytical approach
- Synchrotron Radiation Image
  - ray-tracing and GR relativistic transfer
  - challenge
- Summary

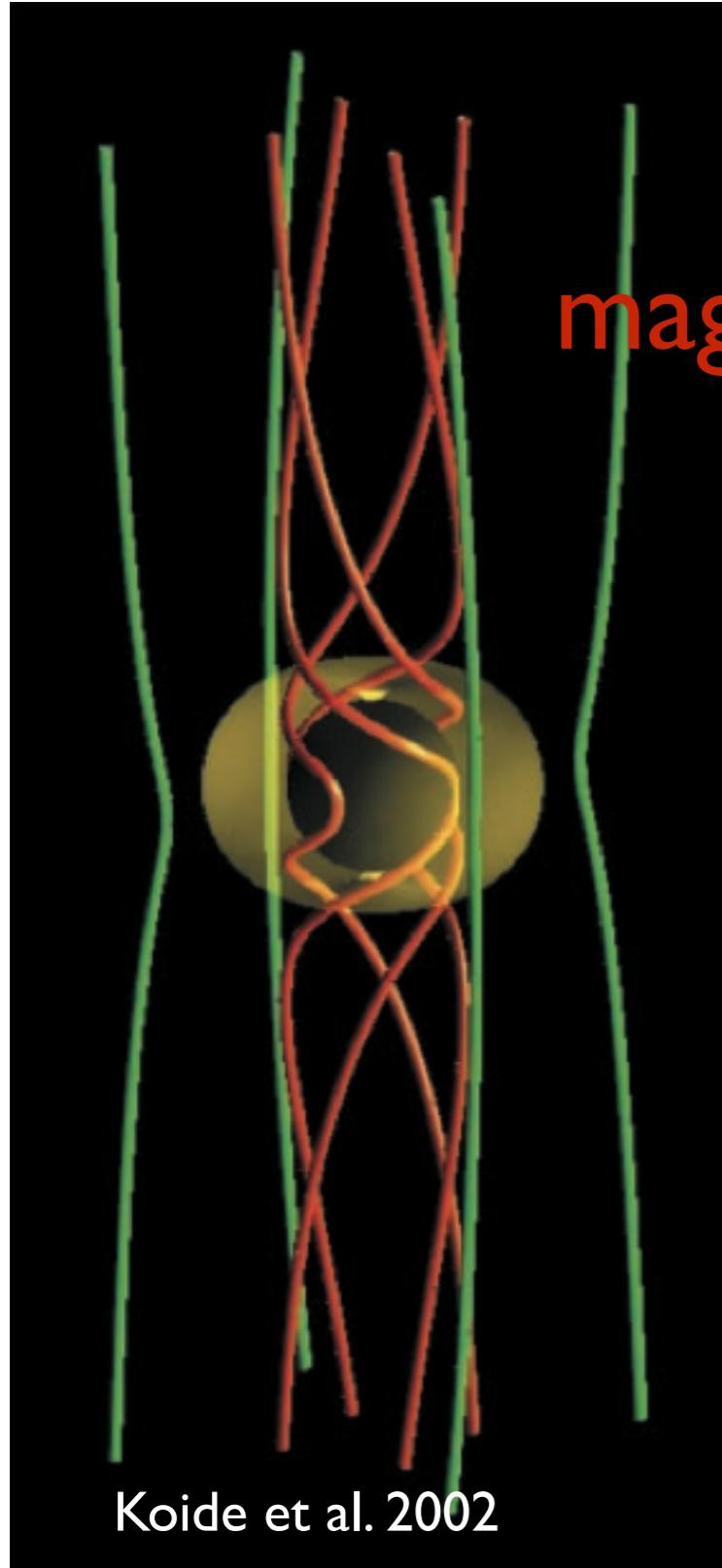
# ergosphere

(the outer boundary is called “static limit”)

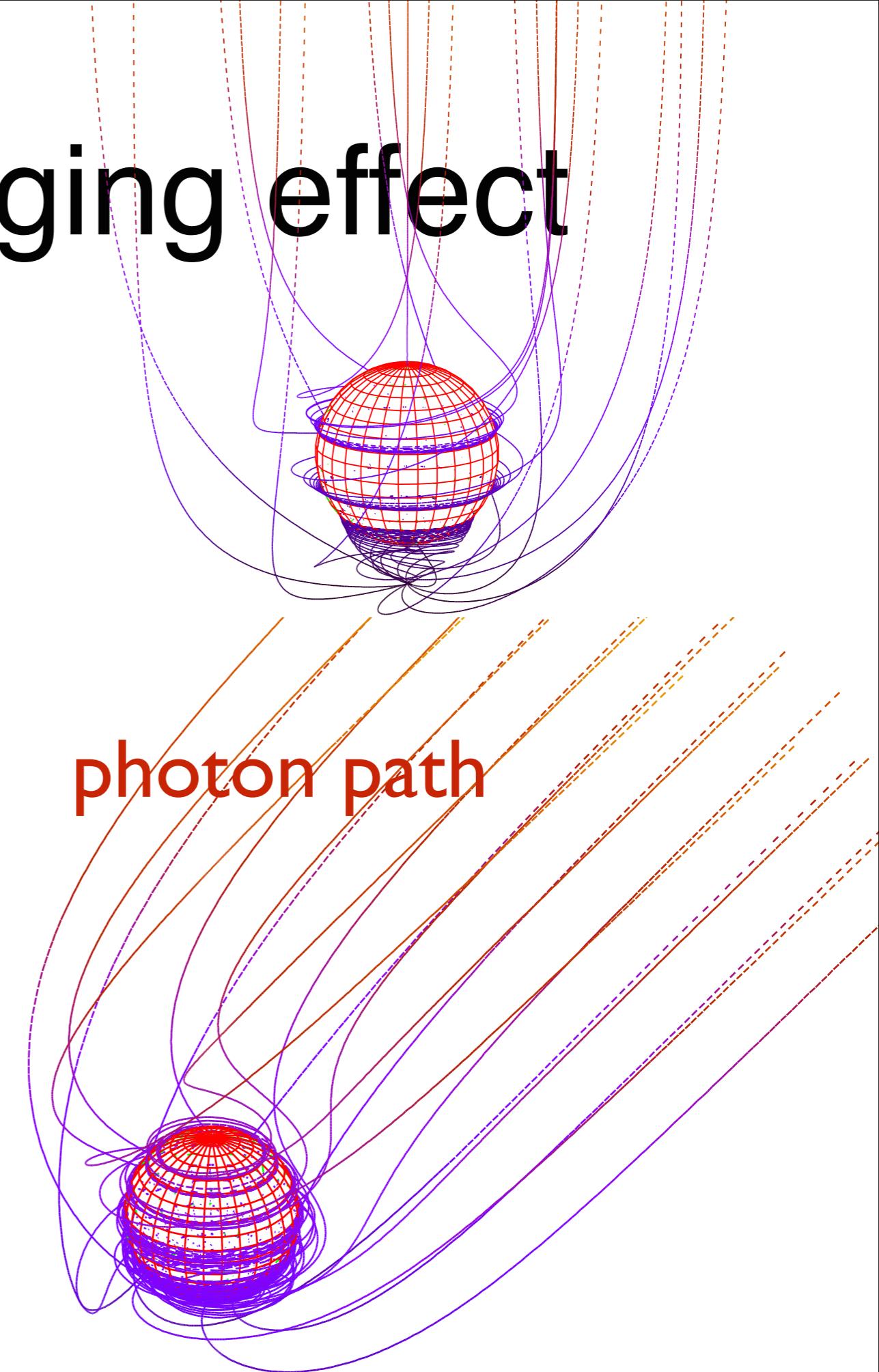


event horizon

# Frame Dragging effect

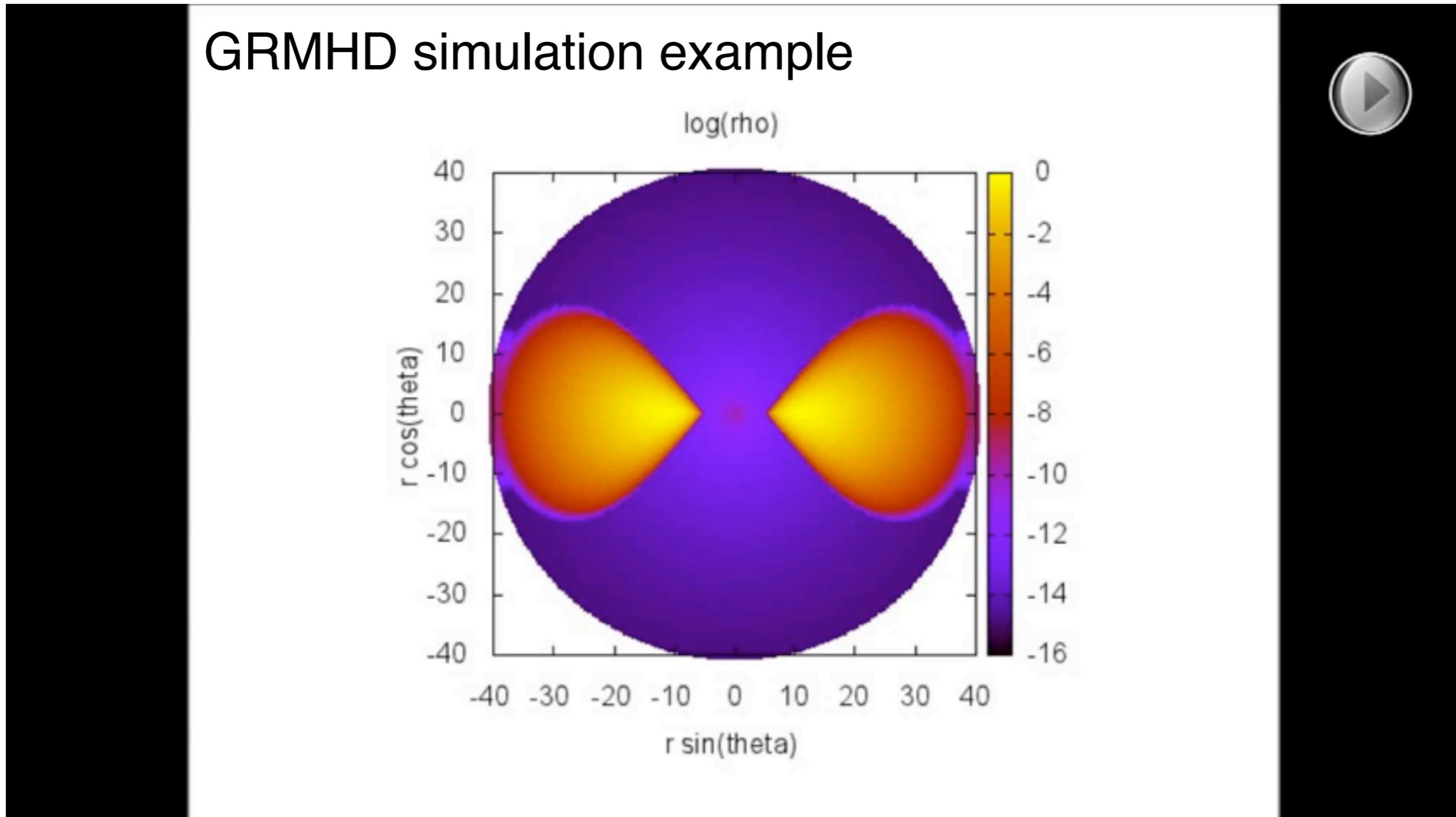


magnetic field

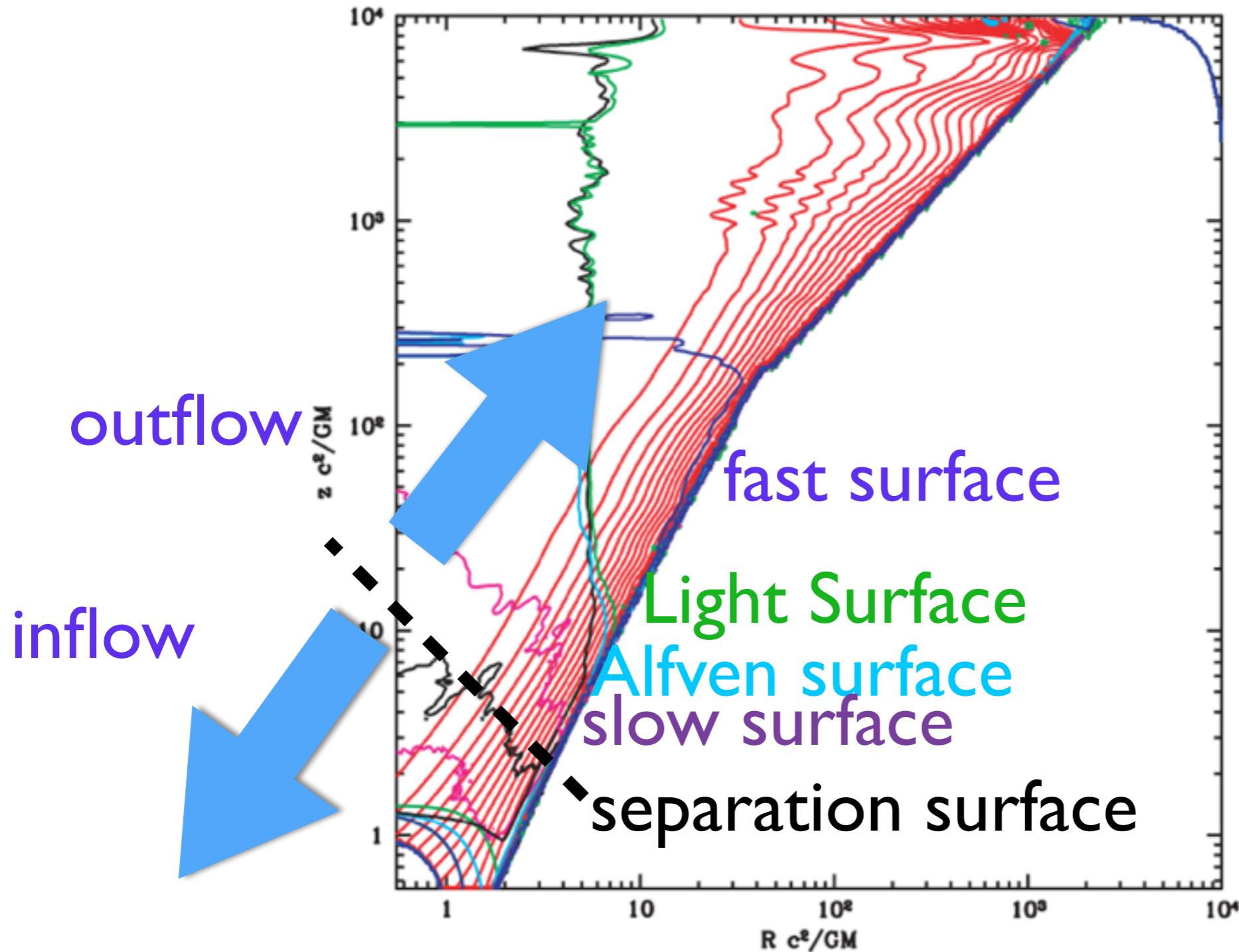


photon path

# Extraction of Black hole Energy: by large scale magnetic field (Blandford & Znajek 1977) by GRMHD flow (Takahashi et al. 1990)



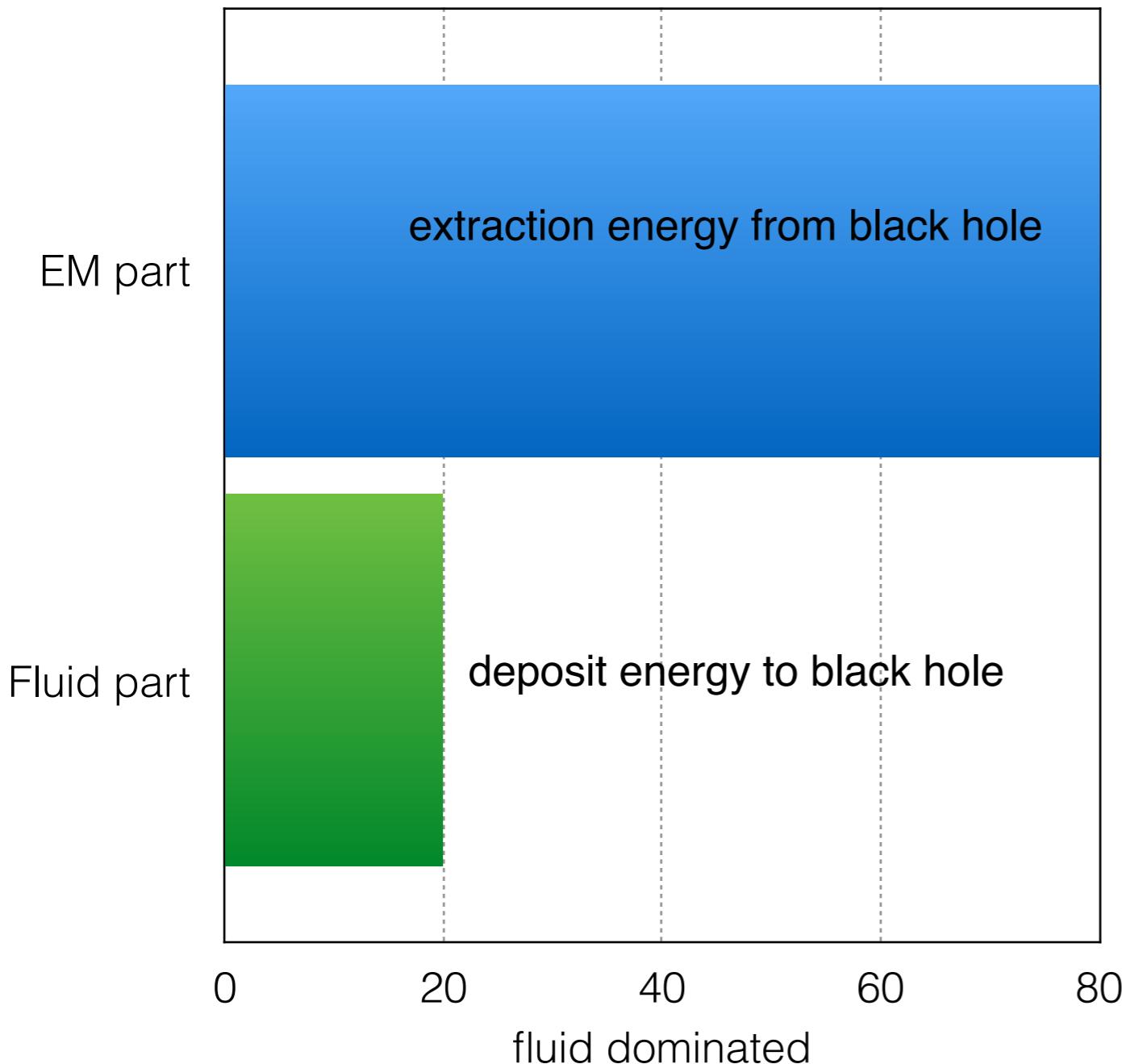
# GRMHD flow structure



time-averaged GRMHD simulation result, McKinney 2006

# inflow

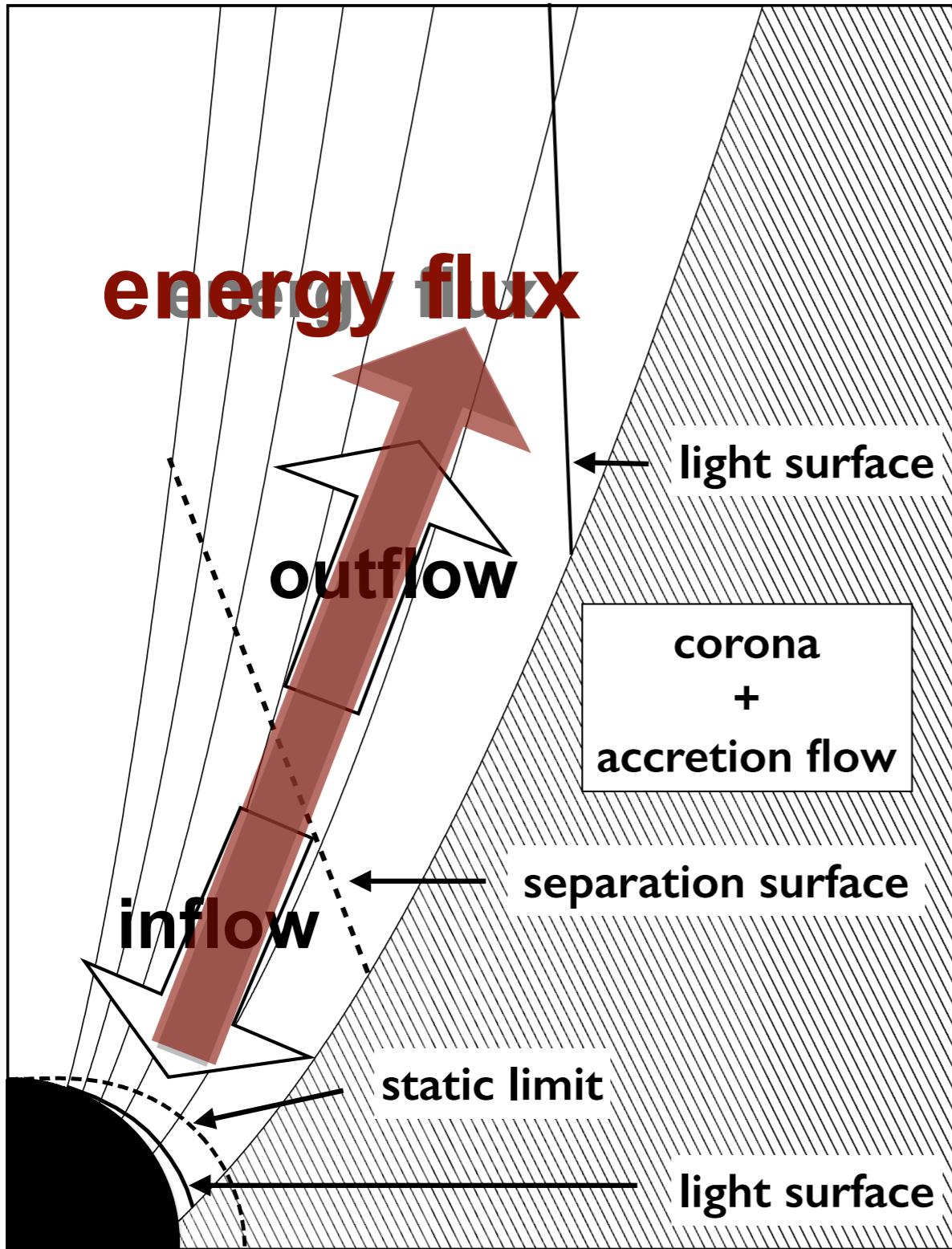
GRMHD inflow



The black hole rotational energy is extracted outward when the flow become magnetically dominated

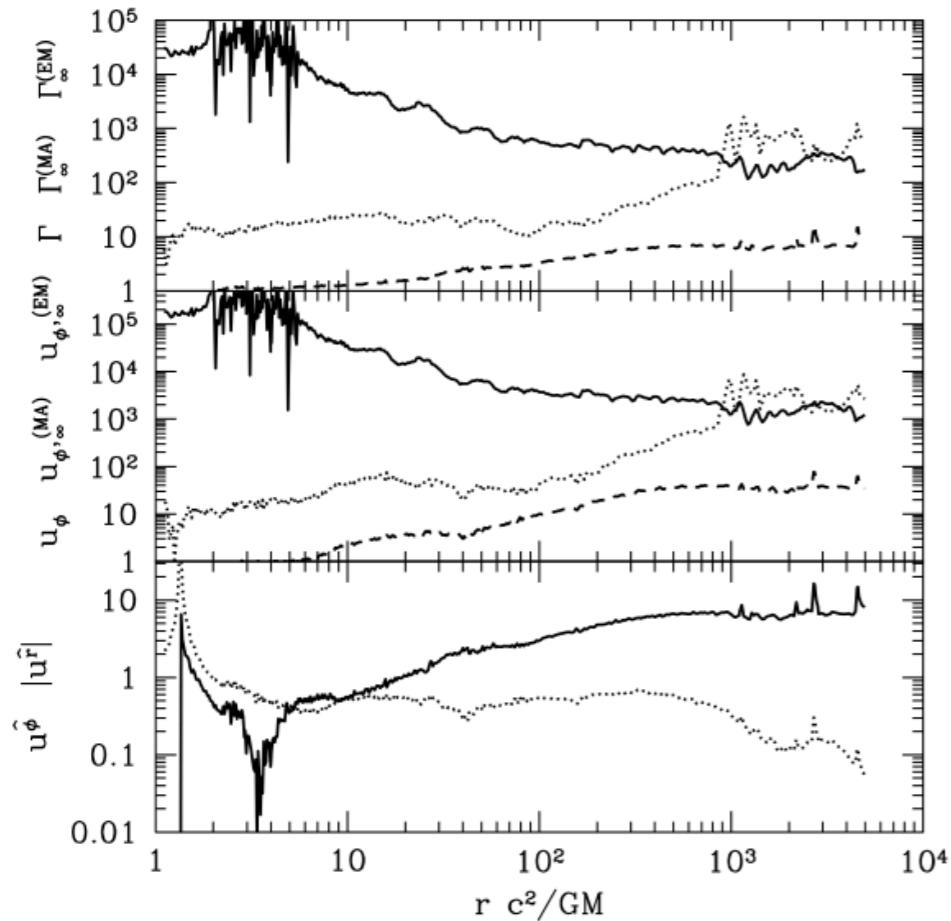
launching and quenching of relativistic jet can be related to the accretion state  
(Pu et al. 2012, Globus & Levinson 2013)

# from inflow to outflow



- focus on **magnetically dominated case**
- the develop of the **outflow** is constraint by the **inflow**, assuming **Poynting energy flux is continuously propagate outward**

# semi-analytical jet model



McKinney 2006 (GRMHD simulation)

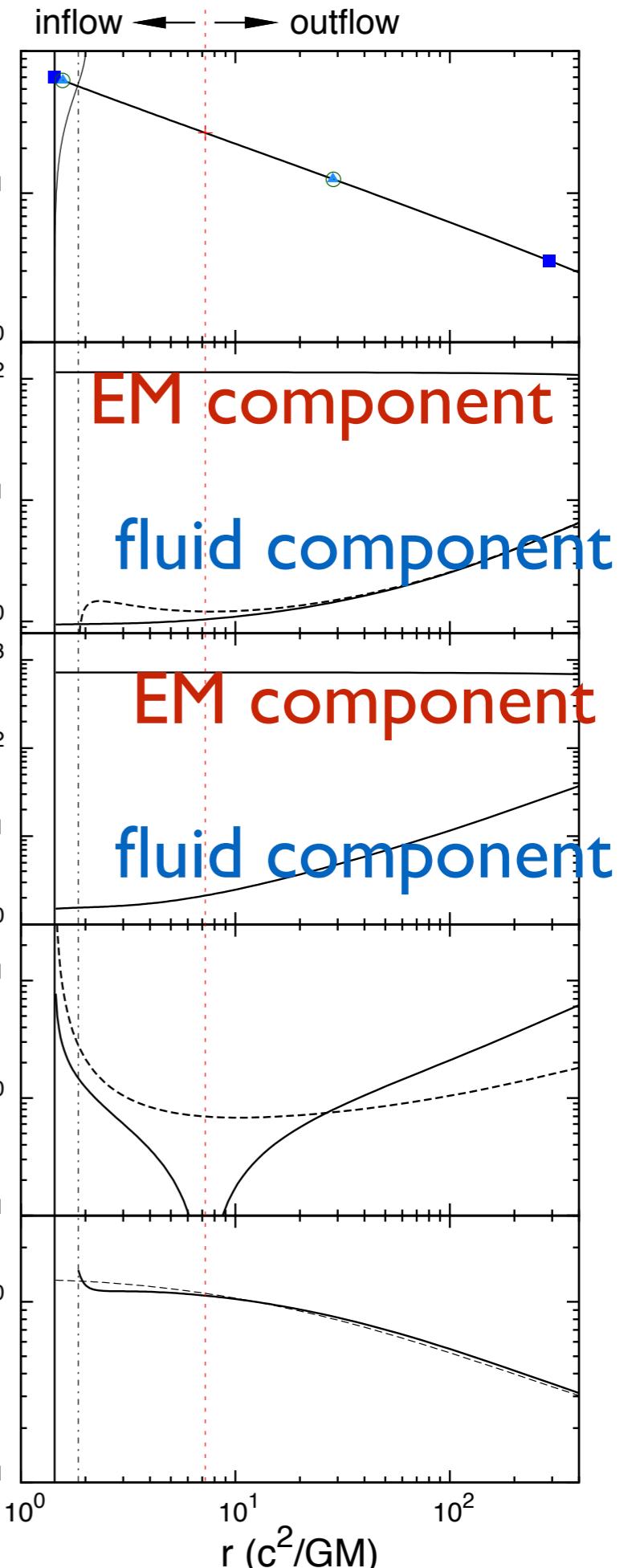
Location of characteristic surfaces

conversion of energy

conversion of angular momentum

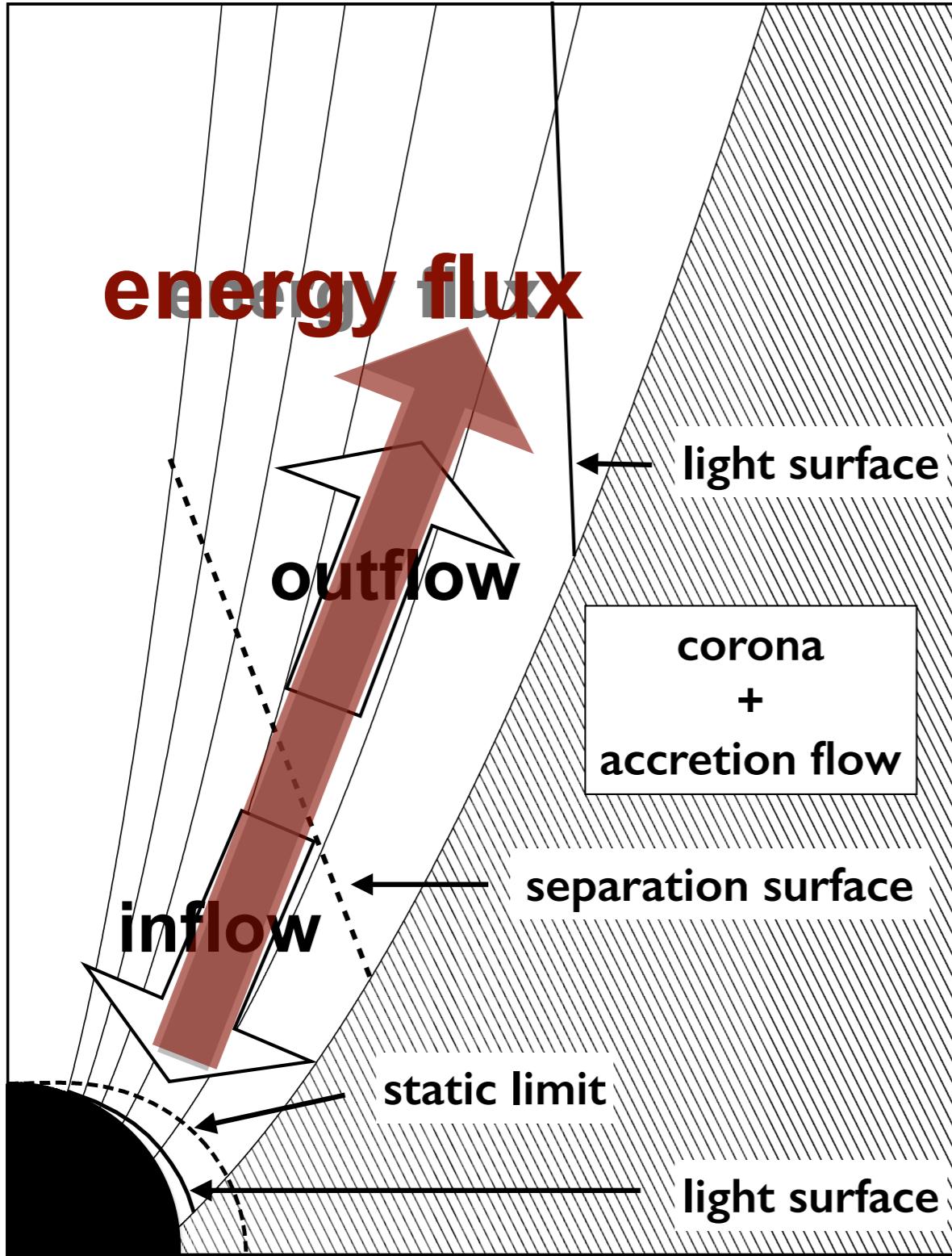
dynamical structure

pitch angle

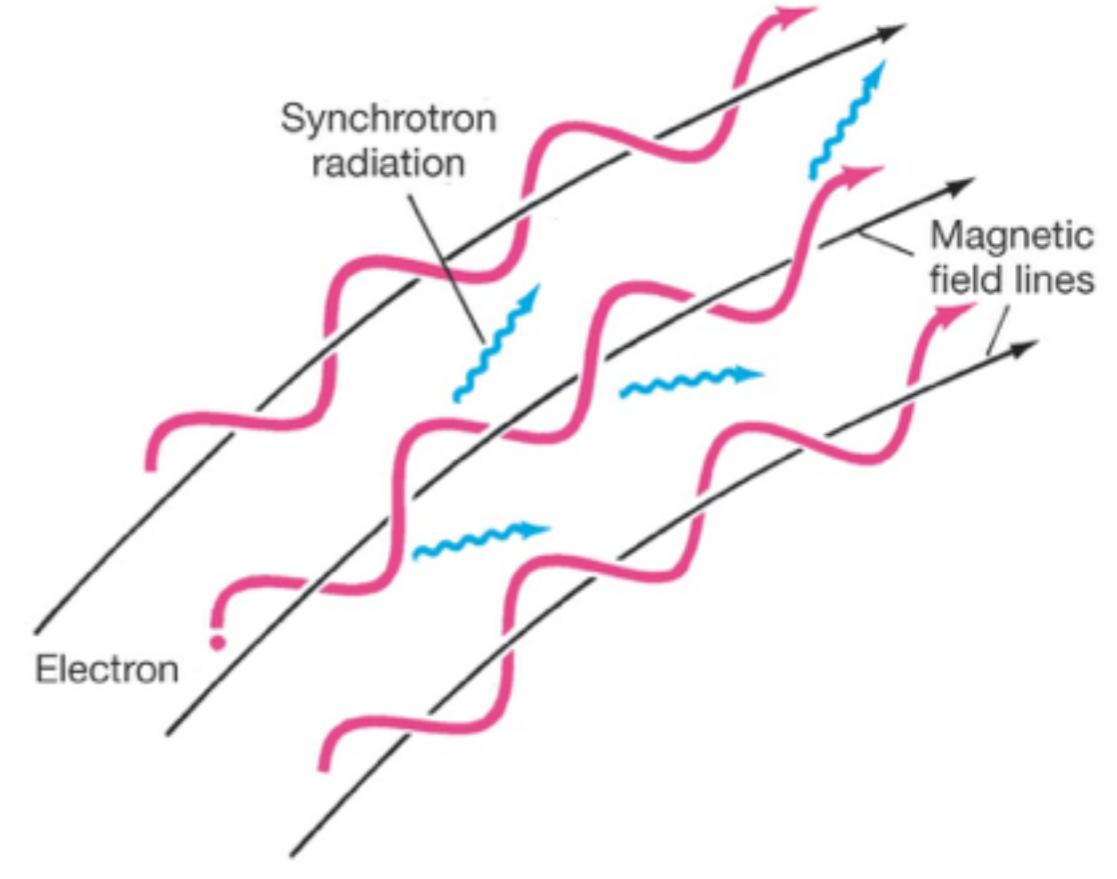


Pu et al. 2015 (semi-analytical solution)

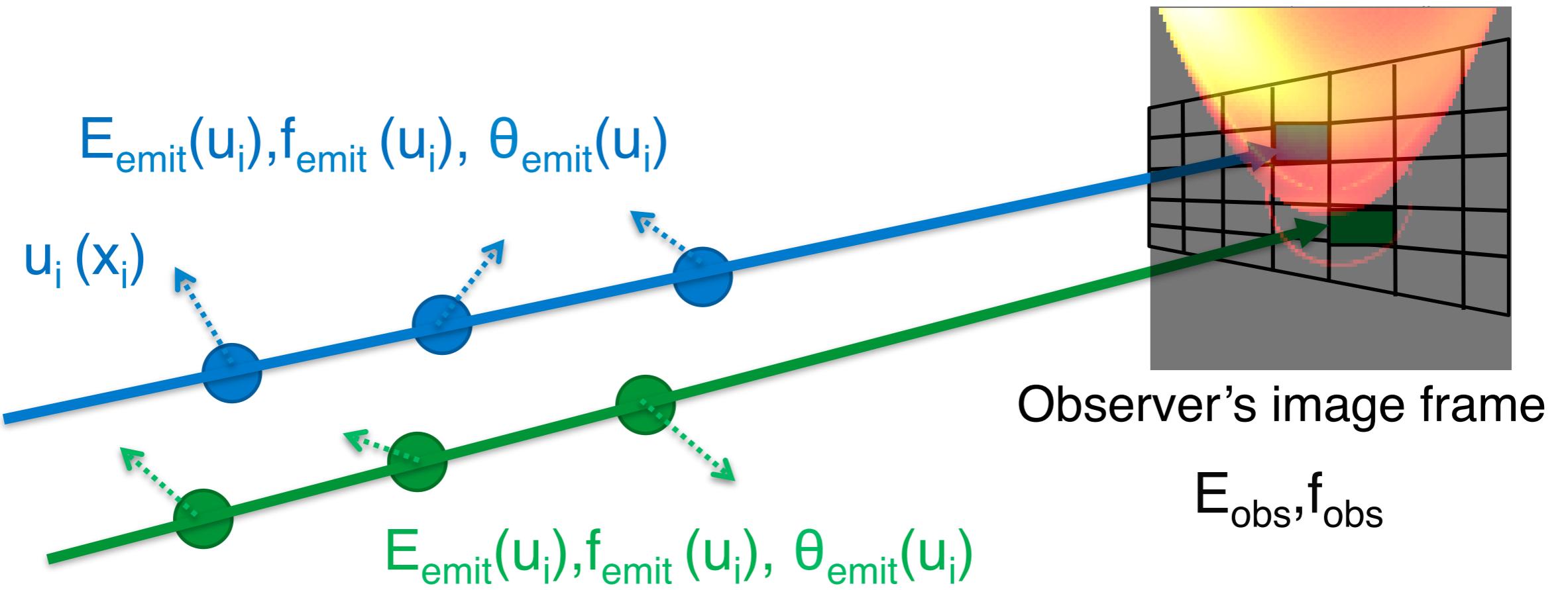
# Radiation!



jet emission at **sub-mm** is mainly contributed by  
**Synchrotron radiation**



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- **ray tracing** (photon trajectory in curved spacetime)
- **dynamics/distribution of surrounding materials**  
(correction of energy/ frequency/ angle)
- **radiative transfer** (physical process take place locally)

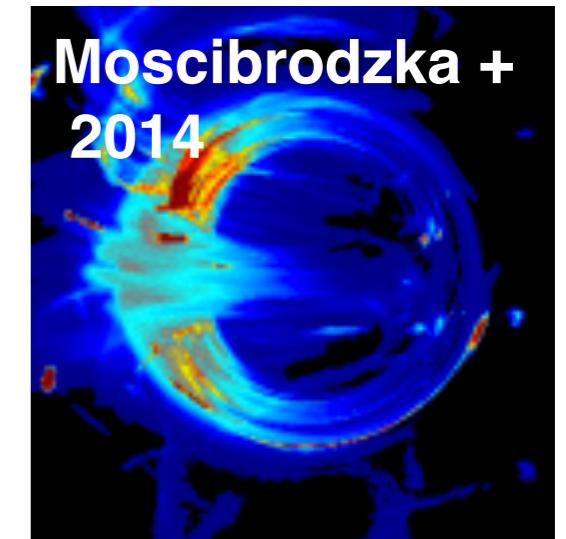
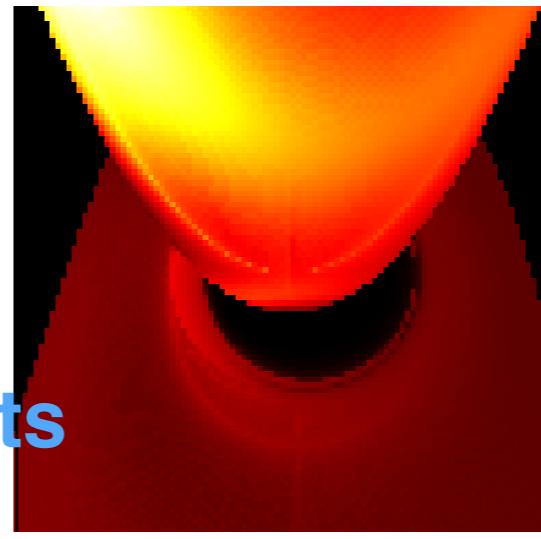
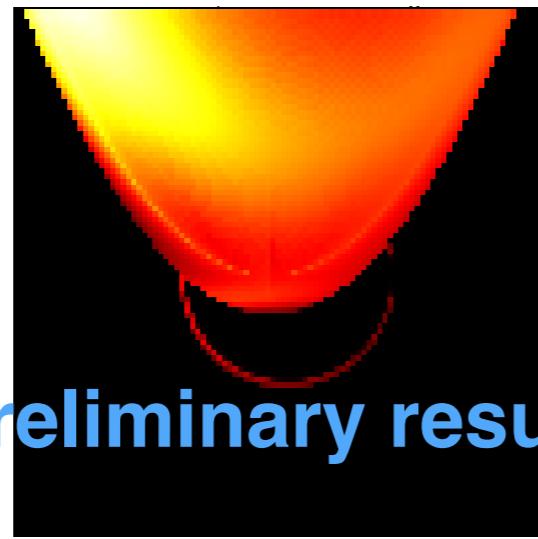
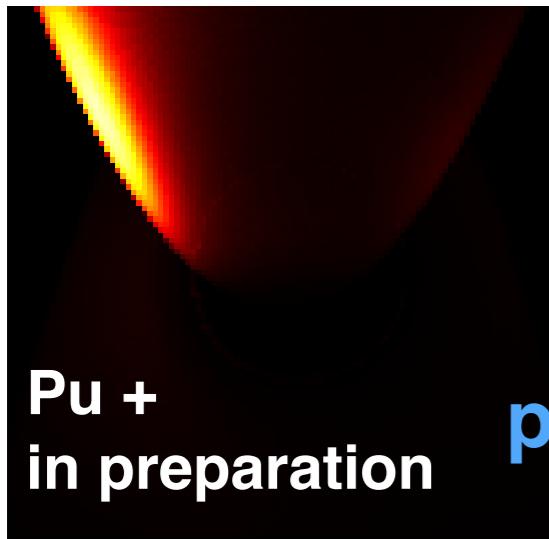
# Synchrotron emission

- thermal (relativistic Maxwellian) energy distribution of electrons
- function of
  - I. electron temperature
  - 2. magnetic field
  - 3. electron number density
- power-law energy distribution of electrons
- function of:
  - I. energy cut off
  - 2. power-law index
  - 3. magnetic field
  - 4. electron number

**significant uncertainties!**

# Zoology of Jet Images

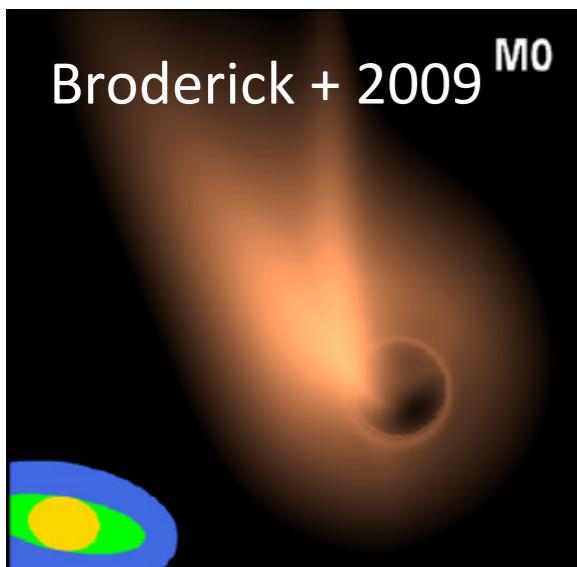
- semi-analytical GRMHD jet model



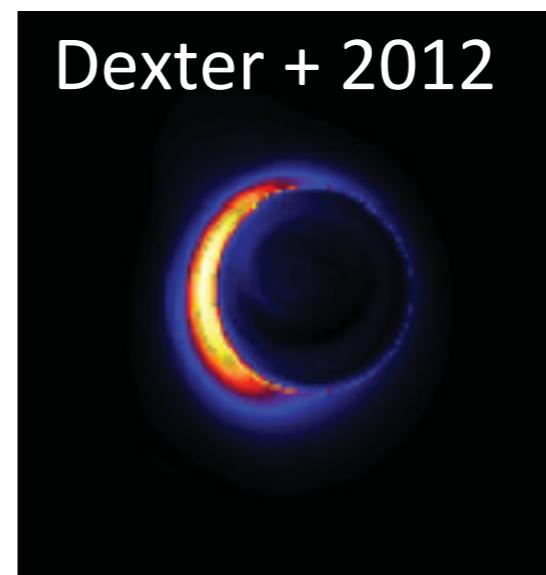
- non-thermal synchrotron

- thermal synchrotron
- isothermal jet

- thermal synchrotron
- isothermal jet + “counter jet”



- thermal + non-thermal synchrotron (disk)
- non-thermal synchrotron (jet)
- semi-analytical force-free jet model



- thermal synchrotron (disk)
- non-thermal synchrotron (jet)
- post processing of GRMHD simulation results

# even more challenge...

- time-dependent feature  
(need to consider light-crossing time)
- evolution of electron energy distribution
- non equal-partition between the field and non-thermal electrons
- pair-production?

example of time-dependent ray tracing  
(by Yun and Pu)



# Summary

- GRMHD jet model
  - due to frame-dragging effect, jet can be powered by the rotating black hole
  - semi-analytical approach provide a complementary understanding of the relativistic jets, compared to GRMHD numerical simulations (e.g. free from numerical dissipation)
- Synchrotron Radiation Image
  - important for upcoming sub-mm VLBI observation will reach micro-arcsec resolution
  - very challenge! (uncertain electron properties)